

11.7b Surface Area prisms and cylinders with work

Prism: Surface Area

- Lateral: $L = Ph$



- Total: $T = Ph + 2B$



Cylinder: Surface Area

- Lateral: $L = 2\pi rh$



- Total: $T = 2\pi rh + 2\pi r^2$

Right Prism vs Oblique Prism



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Example 1

- Find the surface area of this prism if the height is 8 cm?

$$\begin{aligned} LA &= Ph \\ &= (7+6+6)(8) \\ &= 152 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} T &= LA + 2B = LA + \frac{1}{2}bh \\ &= 152 + \frac{1}{2}(7)(\sqrt{23.75}) \\ &= 169.057 \text{ cm}^2 \end{aligned}$$

Diagram of a triangular prism with a right-angled triangular base. The vertical leg is labeled 7 units, the horizontal leg is labeled 6 units, and the hypotenuse is labeled 8 units. The height of the prism is also labeled 8 units.

Example 2

- Find the surface area to the nearest tenth of the prism below.

$$\begin{aligned} L &= Ph \\ T &= Ph + 2B \end{aligned}$$

$$L = (7+8+9+12)(10)$$

$$= 360 \text{ in}^2$$

$$\begin{aligned} T &= LA + 2B = LA + 2\left(\frac{1}{2}(b_1+b_2)h\right) \\ &= 360 + 2\left(\frac{1}{2}(8+12)(6)\right) = 480 \text{ in}^2 \end{aligned}$$

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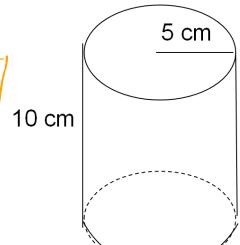
Example 3

- Find the exact surface area of the right cylinder.

$$L = 2\pi rh \text{ or } T = 2\pi rh + 2\pi r^2$$

$$L = 2\pi(5)(10) = 100\pi \text{ cm}^2$$

$$\begin{aligned} T &= 100\pi + 2\pi(5)^2 \\ &= 100\pi + 50\pi \\ &= 150\pi \text{ cm}^2 \end{aligned}$$



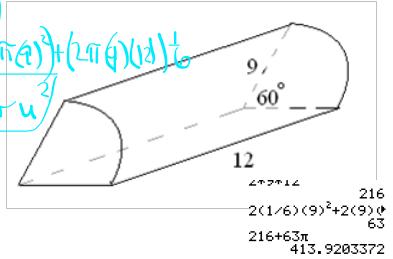
Example 4

- Find the total area of the solid shown.

$$SA = 2\square + \frac{1}{2}\square$$

$$= 2(9)(12) + \frac{1}{2}(6\pi)(12)$$

$$\begin{aligned} &= 216 + 63\pi \text{ in}^2 \\ &\approx 413.920 \text{ in}^2 \end{aligned}$$



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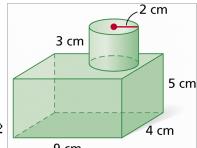
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Example 5

Find the surface area of the composite figure.

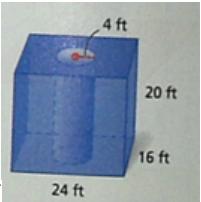
$$\begin{aligned}
 T &= \boxed{[]} + \boxed{[]} - 20 \\
 &= (Ph + 2B) + (2\pi rh + 2\pi r^2) - 2\pi r^2 \\
 &= (2+4+4\pi)(5) + 2(6\cdot 4) \\
 &\quad + (2\pi(2)(3) + 2\pi(2)^2) \\
 &\quad - 2\pi(2)^2 \\
 &= 202 + 20\pi - 8\pi = 202 + 12\pi \text{ cm}^2 \approx 239.699 \text{ cm}^2
 \end{aligned}$$



Example 6

Find the surface area of the composite figures. Round to the nearest tenth.

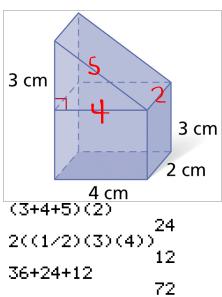
$$\begin{aligned}
 T &= \boxed{[]} - 20 + \boxed{[]} \\
 &= (Ph + 2B) - (2\pi r^2) + (2\pi rh) \\
 &= [24+24+16+16](2) + 2(4\cdot 18) \\
 &\quad - 2\pi(4)^2 + 2\pi(4)(20) \\
 &= 2368 - 32\pi + 160\pi \\
 &= 2368 + 128\pi \text{ ft}^2 \approx 1965.876 \text{ ft}^2
 \end{aligned}$$



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Find the surface area of the composite figures.



$$\begin{aligned}
 \text{TSA} &= \boxed{[]} - 2B + \boxed{[]} \\
 &= Ph + Ph + 2\frac{1}{2}bh \\
 &= (4+4+2)(3) + (3+4+5)(2) + 2\left(\frac{1}{2}(3)(5)\right) \\
 &= 36 + 24 + 12 \\
 &= 72 \text{ cm}^2
 \end{aligned}$$

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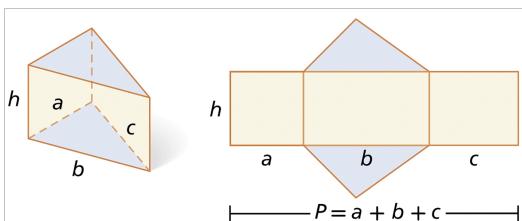
Find the surface area of the composite figures.

$$\begin{aligned}
 \text{TSA} &= \boxed{[]} + \boxed{[]} LA \\
 &= Ph + 2B + Ph \\
 &= (35\cdot 2 + 20\cdot 2)(15) + 2(35\cdot 20) \\
 &\quad + (21\cdot 2 + 18\cdot 2)(9) \\
 &= 1650 + 1400 + 702 \\
 &= 3752 \text{ m}^2
 \end{aligned}$$

Hint: move prism to check answer!!

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The **net** of a right prism can be drawn so that the lateral faces form a rectangle with the same height as the prism. The base of the rectangle is equal to the perimeter of the base of the prism.



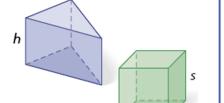
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Lateral Area and Surface Area of Right Prisms

The lateral area of a right prism with base perimeter P and height h is $L = Ph$.

The surface area of a right prism with lateral area L and base area B is $S = L + 2B$, or $S = Ph + 2B$.

The surface area of a cube with edge length s is $S = 6s^2$.



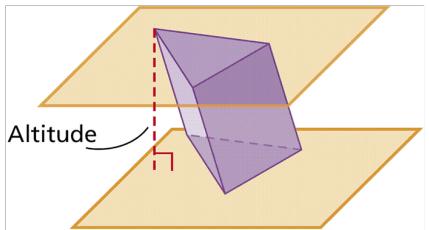
The surface area of a right rectangular prism with length ℓ , width w , and height h can be written as $S = 2\ell w + 2wh + 2\ell h$.

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Caution!

The surface area formula is only true for right prisms. To find the surface area of an oblique prism, add the areas of the faces.



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