

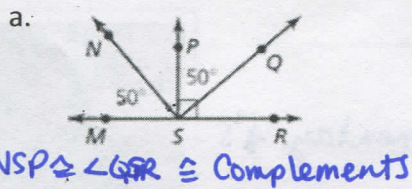
CYU 2.6 Geometric Reasoning DAY ONE

- Use when you get it right all by yourself
- S** Use when you did it all by yourself, but made a silly mistake
- H** Use when you could do it alone with a little help from teacher or peer
- G** Use when you completed the problem in a group
- X** Use when a question was attempted but wrong (get help)
- N** Use when a question was not even attempted

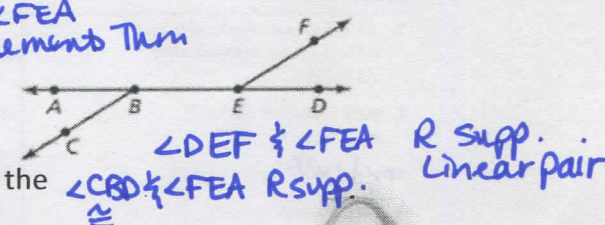
CONCEPTS	BASIC	INTERMEDIATE	ADVANCED
Addition/Subtraction POE/POC	1, 3	3, 6, 7	3, 8
Multiplication/Division POE/POC	3	3	3
Substitution POE		7	8
Transitive POE/POC		6, 7	4, 8
Def. of Complementary/Supplementary Angles	2	3, 5, 7	3, 6, 8
Def. of Complement/Supplement	1	3, 5, 7	3, 6
Def. of Congruent Angles/Segments	1, 2	3, 5, 7	3, 6, 8
Def. of Linear Pairs/Def. of Vertical Angles	1, 2	3	3, 4, 8

1. Identify the pair(s) of congruent angles in the figures. Explain how you know they are congruent.

$\angle MSN \cong \angle PSQ$
Def of \cong
 $\angle MSP \cong \angle PSR$
Def of Rt \angle 's

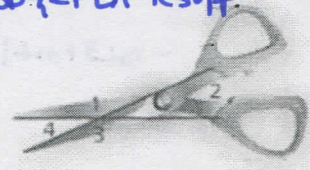


b. $\angle ABC$ is supplementary to $\angle CBD$. $\angle ABC \cong \angle DEF$
 $\angle CBD$ is supplementary to $\angle DEF$. \cong Supplements Thm
 $\angle CBD \cong \angle FEA$
 \cong Supplements Thm

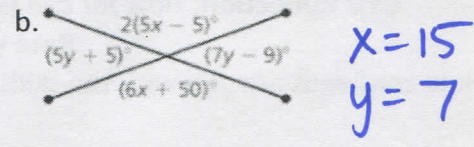
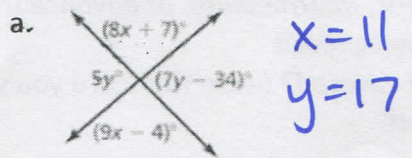


2. Use the diagram and the given angle measure to find the other three measures.

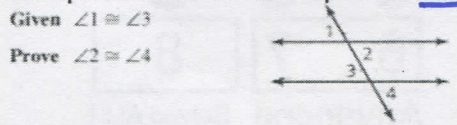
- a. $m\angle 1 = 143^\circ$ $m\angle 2 = 37^\circ$, $m\angle 3 = 143^\circ$, $m\angle 4 = 37^\circ$
 b. $m\angle 3 = 159^\circ$ $m\angle 1 = 159^\circ$, $m\angle 2 = 21^\circ$, $m\angle 4 = 21^\circ$
 c. $m\angle 2 = 34^\circ$ $m\angle 1 = 146^\circ$, $m\angle 3 = 146^\circ$, $m\angle 4 = 34^\circ$



3. Find the values of x and y.



4. Complete the flowchart proof. Then transfer it into a two-column proof.

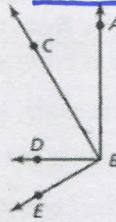


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    graph LR
      A[" $\angle 1 \cong \angle 3$   
Given"] --> B[" $\angle 1 \cong \angle 2, \angle 3 \cong \angle 4$   
Vertical Angles  
Congruence Theorem  
(Theorem 2.6)"]
      B --> C[" $\angle 2 \cong \angle 3$   
Transitive Prop  
(angle)"]
      C --> D[" $\angle 2 \cong \angle 4$   
Transitive Prop  
(angle)"]
    
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5. Complete the two-column proof and then transfer it into a paragraph proof.

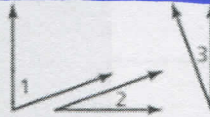
Given $\angle ABD$ is a right angle.
 $\angle CBE$ is a right angle.
 Prove $\angle ABC \cong \angle DBE$



STATEMENTS	REASONS
1. $\angle ABD$ is a right angle. $\angle CBE$ is a right angle.	1. given
2. $\angle ABC$ and $\angle CBD$ are complementary.	2. Definition of complementary angles
3. $\angle DBE$ and $\angle CBD$ are complementary.	3. Def. of complementary \angle 's
4. $\angle ABC \cong \angle DBE$	4. \cong Complements Thm

6. Complete the paragraph proof and then transfer it into a two-column proof.

Given $\angle 1$ and $\angle 2$ are complementary.
 $\angle 1$ and $\angle 3$ are complementary.
 Prove $\angle 2 \cong \angle 3$



$\angle 1$ and $\angle 2$ are complementary, and $\angle 1$ and $\angle 3$ are complementary. By the definition of complementary angles, $m\angle 1 + m\angle 2 = 90^\circ$ and $m\angle 1 + m\angle 3 = 90^\circ$. By the Transitive POE, $m\angle 1 + m\angle 2 = m\angle 1 + m\angle 3$. By the Subtraction Property of Equality, $m\angle 2 = m\angle 3$. So, $\angle 2 \cong \angle 3$ by the definition of $\cong \angle$'s (or. if $= \Rightarrow \cong$).

7. Complete the two-column proof.

Given $\angle 1$ and $\angle 2$ are supplementary.
 $\angle 3$ and $\angle 4$ are supplementary.
 $\angle 1 \cong \angle 4$

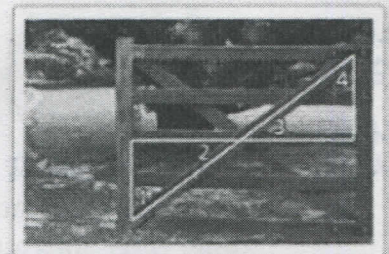


Prove $\angle 2 \cong \angle 3$

STATEMENTS	REASONS
1. $\angle 1$ and $\angle 2$ are supplementary. $\angle 3$ and $\angle 4$ are supplementary. $\angle 1 \cong \angle 4$	1. Given
2. $m\angle 1 + m\angle 2 = 180^\circ$ $m\angle 3 + m\angle 4 = 180^\circ$	2. Def of Supplementary \angle 's
3. <u>$m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$</u>	3. Transitive Property of Equality
4. $m\angle 1 = m\angle 4$	4. Definition of congruent angles
5. <u>$m\angle 1 + m\angle 2 = m\angle 3 + m\angle 1$</u>	5. Substitution Property of Equality
6. <u>$m\angle 2 = m\angle 3$</u>	6. <u>Subtraction POE</u>
7. <u>$\angle 2 \cong \angle 3$</u>	7. <u>if $= \Rightarrow \cong$ (Def. of $\cong \angle$'s)</u>

8. Write a proof using any format.

Given $\angle 1$ and $\angle 3$ are complementary.
 $\angle 2$ and $\angle 4$ are complementary.
 Prove $\angle 1 \cong \angle 4$

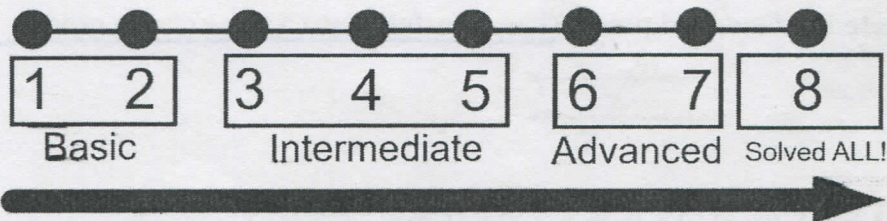


extra paper

CYU Reflection: How far can you go: basic, intermediate, or advanced?

Rate your mastery level!

How confident are you with the skills this CYU covered? Circle the score you would give yourself.



8. Statements	Reasons
1. $\angle 1 \text{ \& } \angle 3$ AND $\angle 2 \text{ \& } \angle 4$ are complementary	1. Given
2. $m\angle 1 + m\angle 3 = 90^\circ$ $m\angle 2 + m\angle 4 = 90^\circ$	2. Def of Complementary \angle 's
3. $m\angle 1 + m\angle 3 = m\angle 2 + m\angle 4$	3. Substitution POE
4. $\angle 2 \cong \angle 3$	4. Def. of vertical \angle 's
5. $m\angle 2 = m\angle 3$	5. If $\cong \Rightarrow =$.
6. $m\angle 1 + m\angle 2 = m\angle 2 + m\angle 4$	6. Substitution POE
7. $m\angle 1 = m\angle 4$	7. Subtraction POE
8. $\angle 1 \cong \angle 4$	8. If $= \Rightarrow \cong$.