

3.4 Perpendicular Line Proofs DAY TWO CYU

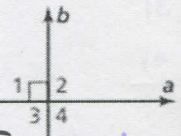
Use when you get it right all by yourself  
*S* Use when you did it all by yourself, but made a silly mistake  
*H* Use when you could do it alone with a little help from teacher or peer  
*G* Use when you completed the problem in a group  
*X* Use when a question was attempted but wrong (get help)  
*N* Use when a question was not even attempted

CONCEPTS	BASIC	INTERMEDIATE	ADVANCED
Perpendicular Lines/Rays/Segments		1, 2, 3	4, 5
Right angles		1, 2, 3	4, 5
Complementary angles		2, 3	4, 5
Angle Add. Postulate		3	4, 5
Parallel Lines			4
Linear Pair/Vertical Angles		1	4, 5
Congruent Angles			4, 5
Line Perpendicular Theorem			4, 5
Perpendicular Transversal Theorem			4, 5
Lines Perpendicular to a Transversal Theorem			4, 5

1. If two intersecting lines are perpendicular, then they intersect to form four right angles.

Given  $a \perp b$

Prove  $\angle 1, \angle 2, \angle 3,$  and  $\angle 4$  are right angles.



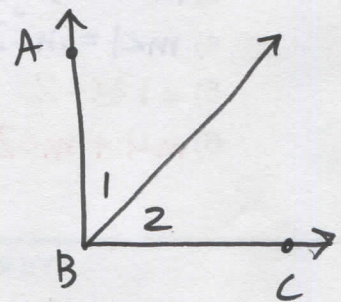
Statements	Reasons	Statements	Reasons
1. $a \perp b$	1. given	8. $m\angle 1 + m\angle 2 = 180$ $m\angle 3 + m\angle 4 = 180$	8. Linear Pair Post.
2. $\angle 1$ is a Rt $\angle$	2. Def of $\perp \iff$	9. $90 + m\angle 2 = 180$ $m\angle 3 + 90 = 180$	9. Substitution POE
3. $\angle 1 \cong \angle 4, \angle 2 \cong \angle 3$	3. Def of Vertical $\angle$ 's	10. $m\angle 2 = 90; m\angle 3 = 90$	10. Subtraction POE
4. $m\angle 1 = 90^\circ$	4. Def of Rt $\angle$	11. $\angle 1, \angle 2, \angle 3,$ & $\angle 4$ are Rt $\angle$ 's	11. Def. of Rt $\angle$ 's
5. $m\angle 1 = m\angle 4$	5. If $\cong \implies =$		
6. $m\angle 4 = 90^\circ$	6. Substitution POE		
7. $\angle 1$ & $\angle 2, \angle 3$ & $\angle 4$ are a linear pair	7. Def of linear pair		

2. If two sides of two adjacent acute angles are perpendicular, then the angles are complementary.

Given  $\overline{BA} \perp \overline{BC}$

Prove  $\angle 1$  and  $\angle 2$  are complementary.

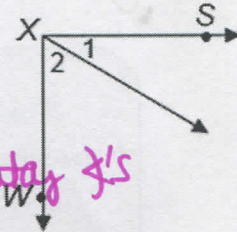
Draw a visual!



Statements	Reasons
1. $\overline{BA} \perp \overline{BC}$	1. Given
2. $\angle ABC$ is a Rt $\angle$	2. Def of $\perp \iff$
3. $m\angle ABC = 90^\circ$	3. Def. of Rt $\angle$ 's
4. $m\angle 1 + m\angle 2 = m\angle ABC$	4. $\angle$ Add. Post.
5. $m\angle 1 + m\angle 2 = 90^\circ$	5. Transitive POE / Substitution POE
6. $\angle 1$ & $\angle 2$ are comp.	6. Def of complementary $\angle$ 's

3. Given:  $\angle 1$  &  $\angle 2$  are Complementary

Prove:  $\overline{SX} \perp \overline{WX}$



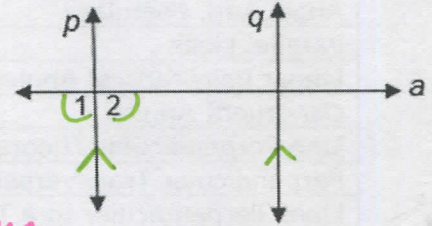
Statements	Reasons
1) $\angle 1$ & $\angle 2$ are Complementary	1) given
2) $m\angle 1 + m\angle 2 = 90$	2) Def. of complementary $\angle$ 's
3) $m\angle WXS = m\angle 1 + m\angle 2$	3) $\angle$ Add. Post.
4) $m\angle WXS = 90$	4) Substitution POE
5) $\angle WXS$ is right	5) Def of Rt $\angle$ 's
6) $\overline{SX} \perp \overline{WX}$	6) Def of $\perp$

Reasons
1) given
2) Def. of complementary $\angle$ 's
3) $\angle$ Add. Post.
4) Substitution POE
5) Def of Rt $\angle$ 's
6) Def of $\perp$

4. Given:  $\angle 1 \cong \angle 2$

$p \parallel q$

Prove:  $q \perp a$



Statements	Reasons
1) $\angle 1 \cong \angle 2; p \parallel q$	1) given
2) $p \perp a$	2) Linear pair $\perp$ Thm

Reasons
1) given
2) Linear pair $\perp$ Thm

5. Prove the statement: If two coplanar lines are perpendicular, then they form a pair of congruent, supplementary angles.

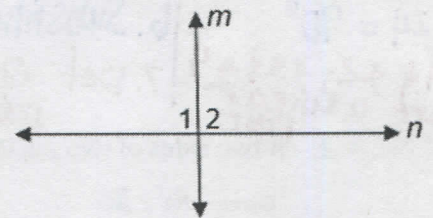
First write the given(hypothesis) and the prove(conclusion) using the diagram.

Given:  $m \perp n$

Prove:  $\angle 1 \cong \angle 2$  and  $m\angle 1 + m\angle 2 = 180^\circ$

Statements	Reasons
1) $m \perp n$	1) given
2) $\angle 1 \cong \angle 2$ R Rt $\angle$ 's	2) Def of $\perp \Leftrightarrow$
3) $m\angle 1 = 90^\circ; m\angle 2 = 90^\circ$	3) Def. of Rt $\angle$ 's
4) $m\angle 1 = m\angle 2$	4) Substitution POE
5) $\angle 1 \cong \angle 2$	5) $IF = \Rightarrow \cong$
6) $m\angle 1 + m\angle 2 = 180^\circ$	6) Def of Linear Pair (Linear Pair Post.)

Reasons
1) given
2) Def of $\perp \Leftrightarrow$
3) Def. of Rt $\angle$ 's
4) Substitution POE
5) $IF = \Rightarrow \cong$
6) Def of Linear Pair (Linear Pair Post.)



CYU Reflection: How far can you go: basic, intermediate, or advanced?

Rate your mastery level!

How confident are you with the skills this CYU covered? Circle the score you would give yourself.

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1	2	3	4	5	6	7	8
Basic		Intermediate			Advanced		Solved ALL!

