

Adding & Subtracting Polynomials

Combining like terms (CLT). The terms must have the same variable and same exponent to combine the coefficients. When you are done, write your answer in standard form (decreasing by exponent.)

TASK 1: Add & Subtract the Polynomials

1) $3x^3 + 2x^2 - x - 7 + (x^3 - 10x^2 + 8)$

$4x^3 - 8x^2 - x + 1$

3) $2x^3 + 6x^2 - x + 1 - (8x^3 - 3x^2 - 2x + 9)$

$2x^3 + 6x^2 - x + 1 - 8x^3 + 3x^2 + 2x - 9$
 $-6x^3 + 9x^2 + x - 8$

2) $(9y^3 + 3y^2 - 2y + 1) + (-5y^2 + y - 4)$

$9y^3 - 2y^2 - y - 3$

4) $(3z^2 + z - 4) - (2z^2 + 3z)$

$3z^2 + z - 4 - 2z^2 - 3z$
 $z^2 - 2z - 4$

Special Product Patterns

Sum and Difference

$(a + b)(a - b) = a^2 - b^2$

Example

$(x + 3)(x - 3) = x^2 - 9$

Square of a Binomial

$(a + b)^2 = a^2 + 2ab + b^2$

Example

$(y + 4)^2 = y^2 + 8y + 16$

$(a - b)^2 = a^2 - 2ab + b^2$

$(2t - 5)^2 = 4t^2 - 20t + 25$

Cube of a Binomial

$(a + b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$

Example

$(z + 3)^3 = z^3 + 9z^2 + 27z + 27$

$(a - b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$

$(m - 2)^3 = m^3 - 6m^2 + 12m - 8$

TASK 2: Multiplying Polynomials

a) $(a + 2b)^3 = (a + 2b)(a + 2b)(a + 2b)$

$(a^2 + 2ab + 2ab + 4b^2)(a + 2b)$
 $a^3 + 2a^2b + 4a^2b + 8ab^2 + 2ab^2 + 8b^3$

b) $(y^2 - 7y + 5)(y^2 - y - 3)$

$y^4 - 8y^3 + 9y^2 + 16y - 15$

c) $(a - 3)(2 - 5a + a^2)$

$2a - 5a^2 + a^3 - 6 + 15a - 3a^2$
 $-6 + 17a - 8a^2 + a^3$

$a^3 - 8a^2 + 17a - 6$

Binomial Expansion	Pascal's Triangle (Coefficients)
$(a+b)^0 = 1$	1
$(a+b)^1 = a+b$	1 1
$(a+b)^2 = a^2 + 2ab + b^2$	1 2 1
$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$	1 3 3 1
$(a+b)^4 = a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4$	1 4 6 4 1
$(a+b)^5 = a^5 + 5a^4b + 10a^3b^2 + 10a^2b^3 + 5ab^4 + b^5$	1 5 10 10 5 1

a ↓
b ↑

TASK 3: Pascal's Triangle

a) $(k-5)^3$
 $a = k$ $b = -5$
 $1k^3(-5)^0 + 3k^2(-5)^1 + 3k(-5)^2 + (-5)^3$
 $k^3 - 15k^2 + 75k - 125$

b) $(6m-8)^3$

$a = 6m$ $b = -8$
 $1(6m)^3(-8)^0 + 3(6m)^2(-8)^1 + 3(6m)(-8)^2 + (-8)^3$
 $(6m)(6m)(6m) + 3(6m)(6m)(-8) + 3(6m)(-8)(-8) + (-8)(-8)(-8)$
 $216m^3 - 864m^2 + 1152m - 512$

1 1 1
1 2 1
1 3 3 1

Notes to yourself about what you struggled with so you don't make the same mistake again!!!

- ones on both sides like an upside down V
- "0" is the first 1
- a ↓ to "0" & b ↑ from "0"
- FOIL, Punnett Square into standard form

Still need help with: