

Long Division

$$\begin{array}{r} 2x+3 \overline{) 6-6x^2+4x^3} \\ \underline{-(4x^3+6x^2)} \phantom{+0x+6} \\ -12x^2+0x+6 \\ \underline{-(-12x^2-18x)} \phantom{+6} \\ 18x+6 \\ \underline{-18x+27} \\ -21 \end{array}$$

$$\begin{array}{r} (12x^4 - 11x^2 + 10) \div (3x^2 + 1) \\ 4x^2 - 5 \\ \underline{12x^4 + 0x^2 + 10} \\ -12x^4 + 0x^2 + 10 \\ \underline{-(-12x^4 + 4x^2)} \\ -15x^2 + 0x + 10 \\ \underline{-(-15x^2 + 10)} \\ 15 \end{array}$$

$$\begin{array}{r} x+2 \overline{) x^2+5x-7} \\ \underline{-(x^2+3x)} \phantom{-7} \\ 2x-7 \\ \underline{-2x+6} \\ -13 \end{array}$$

$$\boxed{x+2 - \frac{13}{x+3}}$$

Synthetic Division

In synthetic division, the degree of the quotient is always one less than the degree of the divisor. Replace missing terms with zeros!!

$$\begin{array}{r} x+3 \overline{) x^2+5x-7} \\ -3 \downarrow 1 \quad 5 \quad -7 \\ + \phantom{1} \quad 2 \quad 13 \\ \hline 1 \quad 2 \quad 13 \end{array}$$

$$\boxed{x+2 \text{ R. } -13}$$

$$(2x^3 - x - 7) \div (x + 3)$$

$$\begin{array}{r} -3 \downarrow 2 \quad 0 \quad -1 \quad -7 \\ + \phantom{-3} \downarrow -6 \quad 18 \quad -51 \\ \hline 2 \quad -6 \quad 17 \quad -58 \end{array}$$

$$\boxed{2x^2 - 6x + 17 \text{ R. } -58}$$

$$x-1 \overline{) 2x^3 - 6x + 5}$$

$$\begin{array}{r} 2 \downarrow 2 \quad 0 \quad -6 \quad 5 \\ + \phantom{2} \downarrow 2 \quad 2 \quad -4 \\ \hline 2 \quad 2 \quad -4 \quad 1 \end{array}$$

$$\boxed{2x^2 + 2x - 4 + \frac{1}{x-1}}$$

### Synthetic Substitution

In synthetic substitution, you plug in the value of  $x$  provided to all  $x$ 's in the function. Your answer is a coordinate. Be sure to show the set-up to earn full credit, but use your calculator to get the answer.

$$P(x) = 2x^4 - 3x^3 + 4x^2 - 5x + 1, \text{ find } P(2).$$

$$P(2) = 2(2)^4 - 3(2)^3 + 4(2)^2 - 5(2) + 1$$

$$P(2) = 15$$
$$(2, 15)$$

$$F(x) = x^4 - 3x^2 + 4x - 5, \text{ find } F(-2)$$

$$F(-2) = (-2)^4 - 3(-2)^2 + 4(-2) - 5$$

$$F(-2) = -9$$
$$(-2, -9)$$

Notes to yourself about what you struggled with so you don't make the same mistake again!!

- Don't forget the zeros as place holders

- Show work!

Still need help with: