

### 5.1 $n^{\text{th}}$ Roots & Rational Exponents CYU

Use when you get it right all by yourself

**S** Use when you did it all by yourself, but made a silly mistake

**H** Use when you could do it alone with a little help from teacher or peer

**G** Use when you completed the problem in a group

**X** Use when a question was attempted but wrong (get help)

**N** Use when a question was not even attempted

CONCEPTS	BASIC	INTERMEDIATE	ADVANCED
Set up the radical	1 - 4		
Simplify nth roots	1 - 4		
Evaluating rational exponents with & w/o calc	5 - 8	9 - 10	
Converting rational exponents to and from radicals	11 - 14		
Evaluating radicals and rational exponents	15 - 18		
Geometry Review	19, 20		
Solving equations with exponents		21 - 23	
Real world problems with exponents			24, 25

Find the indicated real  $n^{\text{th}}$  root(s) of  $a$ .

1.  $n = 3$  &  $a = 8$

2.  $n = 2$  &  $a = 0$

3.  $n = 4$  &  $a = 256$

4.  $n = 5$  &  $a = -32$

Evaluate the expression without using a calculator.

5.  $64^{\frac{1}{6}}$

6.  $25^{\frac{3}{2}}$

7.  $(-243)^{\frac{1}{5}}$

8.  $8^{-\frac{2}{3}}$

**ERROR ANALYSIS** Describe & correct the error in evaluating the expression.

9.  $27^{2/3} = (27^{1/3})^2$   
 $= 9^2$   
 $= 81$

10.  $256^{4/3} = (\sqrt[4]{256})^3$   
 $= 4^3$   
 $= 64$

**MATCHING** Using the proper structure, match the equivalent expressions.

11.  $(\sqrt[3]{5})^4$

A.  $5^{-\frac{1}{4}}$

12.  $(\sqrt[4]{5})^3$

B.  $5^{\frac{4}{3}}$

13.  $\frac{1}{\sqrt[4]{5}}$

C.  $-5^{\frac{1}{4}}$

14.  $-\sqrt[4]{5}$

D.  $5^{\frac{3}{4}}$

Evaluate the expression using a calculator. Round your answer to two decimal places when appropriate.

15.  $\sqrt[5]{32,768}$

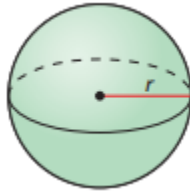
16.  $25^{-\frac{1}{3}}$

17.  $20,736^{\frac{4}{5}}$

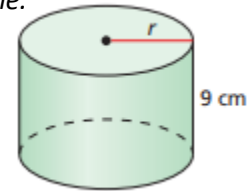
18.  $(\sqrt[4]{187})^3$

**MATHEMATICAL CONNECTIONS** Find the radius of the figure with the given volume.

19.  $V = 216 \text{ ft}^3$



20.  $V = 1332 \text{ cm}^3$



Find the real solution(s) of the equation. Do not round your answer. Leave all answers exact.

21.  $x^6 + 36 = 100$

22.  $x^3 + 40 = 25$

23.  $\frac{1}{6}x^3 = -36$

**PROBLEM SOLVING**

24. A weir is a dam that is built across a river to regulate the flow of water. The flow rate  $Q$  (in cubic feet per second) can be calculated using the formula  $Q = 3.367lh^{\frac{3}{2}}$ , where  $l$  is the length (in feet) of the bottom of the spillway and  $h$  is the depth (in feet) of the water on the spillway. Determine the flow rate of a weir with a spillway that is 20 feet long and has a water depth of 5 feet.



25. The mass of the particles that a river can transport is proportional to the sixth power of the speed of the river normally flows at a speed of 1 meter per second. What must its speed be in order to transport particles that are twice as massive as usual? 10 times as massive? 100 times as massive?

**CYU Reflection:** How far can you go: basic, intermediate, or advanced?

**Rate your mastery level!**

How confident are you with the skills this CYU covered? Circle the score you would give yourself.

