

Solving systems of equations:



5.1: by graphing

5.2: using substitution

What about this system of equations?

$$4x + 3y = 14$$

$$2x - 3y = -23$$

Solving by substitution will be quite "messy"?

Is there another way??

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$$4x + 3y = 14$$

get x by itself?

$$\cancel{4x} = -\frac{3y}{4} + \frac{14}{4}$$

get y by itself?

$$\cancel{3y} = -\frac{4x}{3} + \frac{14}{3}$$

$$2x - 3y = -23$$

get y by itself?

$$\cancel{-3y} = -\frac{2x}{-3} - \frac{23}{3}$$

get x by itself?

$$\cancel{2x} = \frac{3y}{2} - \frac{23}{2}$$

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## 5.3 Solve a System of Equations by Elimination

### What You Will Learn

- ▶ Solve systems of linear equations by elimination.
- ▶ Use systems of linear equations to solve real-life problems.

### Example 1:

Solve the system using elimination.

$$\begin{array}{r} -3x + 4y = 12 \\ + 3x - 6y = 18 \\ \hline \end{array}$$

$$\begin{array}{r} -4y = 30 \\ -2 \\ \hline y = -15 \end{array}$$

$$\begin{array}{r} -3x + 4(-15) = 12 \\ -3x - 60 = 12 \\ +60 \quad +60 \\ \hline \end{array}$$

$$\begin{array}{r} -3x = 72 \\ -3 \\ \hline x = -24 \end{array}$$

$$\boxed{(-24, -15)}$$

$$\begin{array}{r} -3(-24) + 4(-15) = 12 \\ 3(-24) - 6(-15) = 18 \end{array}$$

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$$\begin{array}{r} -3x + 4y = 12 \\ + 3x - 6y = 18 \\ \hline -2y = 30 \\ y = -15 \end{array}$$

Once you know  $y = -15$ , then you can substitute  $-15$  in for  $y$  in either of the two equations.

$$\begin{array}{l} -3x + 4(-15) = 12 \\ -3x - 60 = 12 \\ -3x = 72 \\ x = -24 \end{array}$$

**Final Answer:  $(-24, -15)$**

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Example 2:

Solve by elimination:

$$\begin{array}{r} 2a - 3b = -11 \\ -1 + 3b = 8 \\ \hline 3a = -3 \\ a = -1 \end{array}$$

$$\begin{array}{r} 2a - 3b = -11 \\ + 1a + 3b = 8 \\ \hline 3a = -3 \\ a = -1 \end{array}$$

$$\boxed{(-1, 3)}$$

$$\begin{array}{r} 2(-1) - 3(3) = -11 \\ -1 + 3(3) = 8 \end{array}$$

Example 3:

What about this one?

$$\begin{array}{r} 2x + y = 7 \\ 7x + y = 32 \\ \hline -5x = 25 \\ x = -5 \end{array}$$

$$\begin{array}{r} 2(5) + y = 7 \\ 10 + y = 7 \\ -10 + y = -10 \\ \hline y = -3 \end{array}$$

$$\boxed{(5, -3)}$$

$$\begin{array}{r} 2(5) + (-3) = 7 \\ 7(5) + (-3) = 32 \end{array}$$

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YOUR TURN: Solve for x and y using elimination.

a)  $4x + 2y = 28$   
 $4x - 3y = 18$

$$\begin{array}{r} 4x + 2y = 28 \\ + -4x + 3y = -18 \\ \hline 5y = 10 \\ y = 2 \end{array}$$

$$\begin{array}{r} 4x + 2(2) = 28 \\ 4x + 4 = 28 \\ -4 \quad -4 \\ \hline 4x = 24 \\ x = 6 \end{array}$$

$$\boxed{(6, 2)}$$

b)  $a - 2b = 5$   
 $3a - 2b = 9$

$$\begin{array}{r} -a + 2b = -5 \\ 3a - 2b = 9 \\ \hline 2a = 4 \\ a = 2 \end{array}$$

$$\begin{array}{r} a - 2b = 5 \\ -2 \quad -2 \\ \hline -2b = 3 \\ b = -\frac{3}{2} \end{array}$$

$$\boxed{(2, -\frac{3}{2})}$$

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## 5.3 Day One Worksheet

**A: all**

**B: all**

**C: odds**