

**OBJECTIVE 1: Solving Radical Equations & Inequalities**STEPS:

- Get the radical alone on one side
- Eliminate the radical by raising each side to the power of the index
  - If square root, then square both sides
  - If cube root, then cube both sides
  - If fourth root, then do both sides to the fourth power
- Solve each equation for your variable, usually  $x$
- Check your solution for extraneous solutions
  - Think about domain restrictions
- Restrict your domain, if necessary
  - Rule 1: radicand  $\geq 0$
  - Rule 2: denominator cannot = 0
  - Rule 3: radicand in the denominator  $> 0$

TASK 1: Solve the following equations by following the steps above.

a)  $\sqrt[3]{x-9} = -6$

$$\sqrt[3]{x-9} = -6$$

$$x-9 = (-6)^3$$

$$x-9 = -216$$

$$x = -207$$

b)  $(\sqrt{x+25})^2 = (2)^2$

$$x+25 = 4$$

$$x = -21$$

c)  $\sqrt[3]{2x-5} - 2 = 3$

$$\sqrt[3]{2x-5} - 2 = 3$$

$$\sqrt[3]{2x-5} = 5$$

$$2x-5 = 125$$

$$2x = 130$$

$$x = 65$$

TASK 2: Check for Extraneous Solutions

a)  $(x+1)^2 = (\sqrt{7x+15})^2$

FOIL

$x^2 + 2x + 1 = 7x + 15$

$x^2 - 5x - 14 = 0$

$(x-7)(x+2) = 0$

$x = 7, -2$

$x = 7$

$7+1 = \sqrt{7(7)+15}$

$8 = \sqrt{64} \checkmark$

$-2+1 = \sqrt{7(-2)+15}$

$-1 = \sqrt{-14+15}$

$-1 = \sqrt{1}$

$-1 = 1 \times$

b)  $(\sqrt{2x+7})^2 = (x-4)^2$

FOIL

$2x+7 = x^2 - 8x + 16$

$0 = x^2 - 10x + 9$

$0 = (x-9)(x-1)$

$x = 9, 1$

$x = 9$

$\sqrt{2(9)+7} = 9-4 \checkmark$

$\sqrt{2(1)+7} = 1-4 \times$

**TASK 3:** Solve Equations with Two Radicals

a)  $(10x + 9)^2 = (x + 3)^2$

$10x + 9 = x^2 + 6x + 9$

$0 = x^2 - 4x$

$0 = x(x - 4)$

$x = 0, 4$

b)  $(\sqrt{6} - 2)^2 = (\sqrt{x - 2})^2$

$10 - 4\sqrt{6} = x - 2$

exact:  $12 - 4\sqrt{6} = x$

$x \approx 2.202$

$(\sqrt{6} - 2)(\sqrt{6} - 2)$   
 $\sqrt{36} - 2\sqrt{6} - 2\sqrt{6} + 4$   
 $6 - 4\sqrt{6} + 4$   
 $10 - 4\sqrt{6}$

**OBJECTIVE 2:** Solving Equations with Rational Exponents

**TASK 4:** Solve equations with rational exponents by converting to radicals and following the steps provided above in objective 1.

a)  $(3x)^{\frac{1}{3}} = (-3)^{\frac{1}{3}}$

$3x = -27$

$x = -9$

b)  $(x + 6)^{\frac{1}{2}} = x^{\frac{2}{3}}$

$x + 6 = x^{\frac{4}{3}}$

$0 = x^{\frac{4}{3}} - x - 6$

$0 = (x - 3)(x + 2)$

$x = 3, -2$

$x = 3$

c)  $(x + 2)^{\frac{3}{4}} = 8$

$x + 2 = (\sqrt[4]{8})^{\frac{4}{3}}$

$x + 2 = (2)^{\frac{4}{3}}$

$x + 2 = 16$

$x = 14$

**OBJECTIVE 3:** Solving a Radical Inequality

STEPS:

- 1) Determine if the graph is solid ( $\leq$  or  $\geq$ ) or dashed ( $<$  or  $>$ )
- 2) Determine if you shade above or below the function above ( $>$  or  $\geq$ ) or below ( $<$  or  $\leq$ )
- 3) Follow the same steps from objective 1

**TASK 5:** solve the radical inequalities following the steps above

a)  $2\sqrt{x - 3} \geq 3$

$\sqrt{x - 3} \geq \frac{3}{2}$

$(\sqrt{x - 3})^2 \geq (\frac{3}{2})^2$

$x - 3 \geq \frac{9}{4}$

$x \geq \frac{21}{4}$

b)  $\sqrt[4]{x + 1} < 8$

$(\sqrt[4]{x + 1})^4 < (8)^4$

$x + 1 < 8^4$

$x < 655$

c)  $3\sqrt{x - 4} \leq 8$

$\sqrt{x - 4} \leq \frac{8}{3}$

$(\sqrt{x - 4})^2 \leq (\frac{8}{3})^2$

$x - 4 \leq \frac{64}{9}$

$x \leq \frac{116}{9}$

Still need help with:

$x < 7$

$x \leq 16$