

A rational number is a number that can be written as a quotient of two integers (positive & negative whole numbers.) A rational expression is also a quotient (fraction) of two polynomials.

- Remember your denominator can never equal zero.
- $\frac{0}{k}$  VS  $\frac{N}{0}$ : 0 on top is OK, 0 on bottom is a NO go, not ok.
- $f(x) = \frac{x^2+2}{x-3}$  is a rational function, has  $f(x)$
- $\frac{x^2+2}{x-3}$  is a rational expression, no =

$$( ) \quad 0 < >$$

$$[ ] \quad \bullet \leq \geq$$

**OBJECTIVE 1: Finding the Domain of a Rational Function**

- Just like ANY fraction, if a rational expression has a zero in the denominator it is considered undefined.
- Whenever there is a variable in the denominator we are required to restrict the domain.
- To restrict the domain, you set the denominator with a variable = 0 and solve for the variable.
- The solution is what the variable CANNOT = or the answer would be undefined.

$$\frac{0 \checkmark}{K} \quad \frac{NX}{0}$$

TASK 1: Restrict the domain. Write your answer in interval notation.

a)  $f(x) = \frac{x^2+2}{x-3}$

$$\frac{x-3 \neq 0}{x \neq 3}$$

$$D: (-\infty, 3) \cup (3, \infty)$$

b)  $f(x) = \frac{4x^5 - 3x^2 + 2}{-6}$

no variable in denominator so  $\mathbb{R}$

$$D: (-\infty, \infty)$$

c)  $g(x) = \frac{6x^2+1}{x+3}$

$$\frac{x+3 \neq 0}{x \neq -3}$$

$$D: (-\infty, -3) \cup (-3, \infty)$$

## OBJECTIVE 2: Simplifying Rational Expressions

### STEPS:

- Factor the top and bottom.
- Cancel any factors that are on both top and bottom, one for one.

Factor the numerator and the denominator.

$$\frac{x^2 - 9}{x^2 + x - 6} = \frac{(x-3)(x+3)}{(x-2)(x+3)}$$

Look for common factors.

$$= \frac{(x-3) \cdot \cancel{(x+3)}}{(x-2) \cdot \cancel{(x+3)}}$$

$$= \frac{x-3}{x-2} \cdot \frac{x+3}{x+3}$$

$$= \frac{x-3}{x-2} \cdot 1$$

Write  $\frac{x+3}{x+3}$  as 1.

Multiply to remove a factor of 1.

### TASK 2: Simplify each rational expression.

a)  $\frac{2x^2}{10x^3 - 2x^2} = \frac{\cancel{2x}(5x-1)}{\cancel{2x}(5x-1)}$   
 $\frac{1}{5x-1}$   
 $2x^2 \neq 0$   
 $x \neq 0$   
 $5x-1 \neq 0$   
 $5x \neq 1$   
 $x \neq \frac{1}{5}$   
 D:  $(-\infty, 0) \cup (0, \frac{1}{5}) \cup (\frac{1}{5}, \infty)$

b)  $\frac{x^2+x}{x+1} = \frac{x(x+1)}{\cancel{x+1}}$   
 $\frac{x}{1} = x$   
 $x+1 \neq 0$   
 $x \neq -1$   
 D:  $(-\infty, -1) \cup (-1, \infty)$

c)  $\frac{5z^4}{10z^5 - 5z^4} = \frac{\cancel{5z^4}}{\cancel{5z^4}(2z-1)}$   
 $\frac{1}{2z-1}$   
 $5z^4 \neq 0$   
 $z \neq 0$   
 $2z-1 \neq 0$   
 $2z \neq 1$   
 $z \neq \frac{1}{2}$

### TASK 3: Simplify each rational expression.

a)  $\frac{(2+x)}{(x+2)} = \frac{\cancel{x+2}}{\cancel{x+2}} = 1$   
 D:  $(-\infty, -2) \cup (-2, \infty)$

b)  $\frac{2-x}{x-2} = \frac{-x+2}{x-2} = \frac{-1(x-2)}{\cancel{x-2}}$   
 $\frac{-1}{1} = -1$   
 D:  $(-\infty, 2) \cup (2, \infty)$

c)  $\frac{x+3}{3+x} = \frac{\cancel{x+3}}{\cancel{x+3}} = 1$   
 D:  $(-\infty, -3) \cup (-3, \infty)$

d)  $\frac{3-x}{x-3} = \frac{-x+3}{x-3} = \frac{-1(x-3)}{\cancel{x-3}} = -1$   
 D:  $(-\infty, 3) \cup (3, \infty)$

### Common Mistakes:

All or nothing

$$\frac{x+2}{x} = \frac{\cancel{x}+2}{\cancel{x}} = \frac{1+2}{1} = 3$$

Done

$$\frac{x(x+2)}{2x} = \frac{\cancel{x}(x+2)}{\cancel{2x}} = \frac{x+2}{2}$$

Multiplication  
not + or -

Still need help with: