

TASK 1: Answer the following questions.

a) What is the difference between an expression and an equation?

no =

→ Simplify → Solve

b) When is a fraction undefined?

dividing by 0. $\frac{a}{k}$ $\frac{N}{0}$

The KEY to RATIONAL EXPRESSIONS is FACTORING. FACTORING should ALWAYS be your FIRST STEP!

OBJECTIVE 1: Simplifying Rational Expressions

STEPS:

1. Factor the numerator & denominator completely
2. Cancel any common factors
3. Remember ALL OR NOTHING: a + or - groups the two terms it is touching

TASK 2: Simplify the rational expressions below.

a) $\frac{4x^3y^4}{12x^7y^2}$

$= \frac{4}{12} \cdot \frac{x^3}{x^7} \cdot \frac{y^4}{y^2} = \frac{1}{3} \cdot \frac{1}{x^4} \cdot \frac{y^2}{1} = \frac{y^2}{3x^4}$

b) $\frac{8x^3 - 2x^2}{4x^2 - x}$

$= \frac{2x^2(4x-1)}{x(4x-1)} = \frac{2x^2}{x} = 2x$

OBJECTIVE 2: Multiplying Rational Expressions

STEPS:

1. Factor the numerator & denominator completely
2. Cancel any common factors
3. Remember ALL OR NOTHING: a + or - groups the two terms it is touching

TASK 3: Multiply the rational expressions below. Simplify your final answer completely.

a) $\frac{8x^3}{26xy} \cdot \frac{14y^4}{12x^2}$

$= \frac{112x^3y^4}{312xy}$

$\frac{14y^3}{39}$

b) $\frac{2x^2 - x - 3}{x^2 + x} \cdot \frac{4x^2 + 4x}{2x - 3}$

$= \frac{(2x-3)(x+1)}{x(x+1)} \cdot \frac{4x(x+1)}{(2x-3)} = 4(x+1)$

c) $\frac{4x^2 - 4x}{x^2 + 2x - 3} \cdot \frac{x^2 + x - 6}{4x}$

$= \frac{4x(x-1)}{(x+3)(x-1)} \cdot \frac{(x+3)(x-2)}{4x} = x-2$

OBJECTIVE 3: Dividing Rational Expressions

STEPS:

1. Rewrite the problem as a multiplication problem using Keep Change Flip (KCF)
2. Factor the numerator & denominator completely
3. Cancel any common factors
4. Remember ALL OR NOTHING: a + or - groups the two terms it is touching

TASK 4: Divide the rational expressions below. Simplify your answer completely.

a) $(x^2 - 1) \div \frac{x-1}{x+5}$

$$\frac{1}{(x^2-1)} \cdot \frac{x+5}{x-1}$$
$$\frac{(x+1)\cancel{(x-1)}(x+5)}{(x-1)}$$
$$\boxed{(x+1)(x+5)}$$

b) $\frac{x^2+4x+4}{x+3} \div (x+2)$

$$\frac{x^2+4x+4}{x+3} \cdot \frac{1}{x+2}$$
$$\frac{(x+2)\cancel{(x+2)}}{(x+3)} \cdot \frac{1}{\cancel{(x+2)}}$$
$$\boxed{\frac{x+2}{x+3}}$$

c) $\frac{3x-1}{2x^3-2x} \div \frac{x}{2x^3-2x^2}$

$$\frac{3x-1}{2x^3-2x} \cdot \frac{2x^3-2x^2}{x}$$
$$\frac{3x-1}{2x(x^2-1)} \cdot \frac{2x(x^2-x)}{x}$$
$$\frac{3x-1}{(x+1)(x-1)} \cdot \frac{x\cancel{(x-1)}}{x}$$
$$\boxed{\frac{(3x-1)(x-1)}{(x+1)(x-1)}}$$

Common mistakes:

Still need help with: