

Ch. 4 Test p.307

- 1) False, one solution, no solutions, or infinite solutions.
- 2) False, must make both equations true.
- 3) True, $3 \neq 0$ which is false. So, there are \emptyset .
- 4) False, $3x=0 \Rightarrow$ divide by 3 to get $x=0$. Sub that in to get what $y =$.

$$5. \frac{2(1) - 3(-1)}{2+3} = \frac{5}{5} \checkmark$$

$$6. \frac{4(3) - 3(-4)}{12 + 12} = \frac{24}{24} \checkmark$$

$$\frac{6(1) + (-1)}{6 - 1} = \frac{1}{1} \times$$

NO

$$\frac{4(3) + 5(-4)}{12 - 20} = \frac{-8}{-8} \checkmark$$

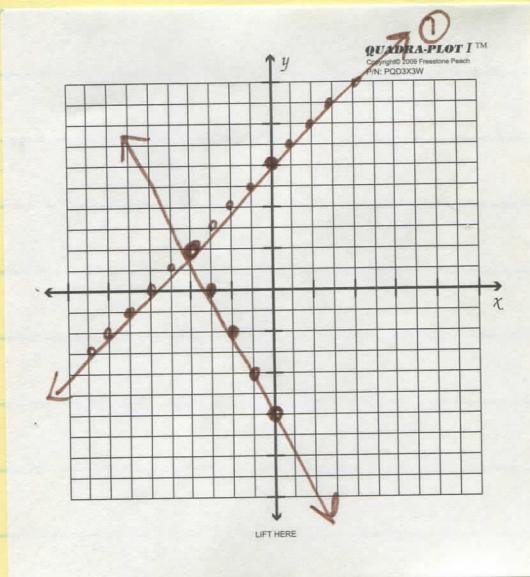
Yes

7.

$$\begin{cases} y - x = 6 \\ y + 2x = -6 \end{cases}$$

$$\begin{aligned} \textcircled{1} \quad y &= x + 6 \\ \textcircled{2} \quad y &= -2x - 6 \end{aligned}$$

(-4, 2)



$$8. \begin{cases} 3x - 2y = -14 \\ x + \frac{3}{2}y = -1 \end{cases} \quad x = (-3y - 1)$$

$$3(-3y - 1) - 2y = -14$$

$$\begin{aligned} -9y - 3 - 2y &= -14 \\ -11y - 3 &= -14 \\ +3 &+ 3 \end{aligned}$$

$$\begin{aligned} -11y &= -11 \\ y &= 1 \end{aligned}$$

(-4, 1)

$$9. \begin{cases} \frac{1}{2}x + 2y = -\frac{15}{4} \\ 4x = -y \quad y = -4x \end{cases}$$

$$\begin{aligned} -y &= 4\left(\frac{1}{2}\right) \\ y &= 2 \\ y &= -2 \end{aligned}$$

$$4 \left[\frac{1}{2}x + 2(-4x) = -\frac{15}{4} \right]$$

$$2x + 8(-4x) = -15$$

$$2x - 32x = -15$$

$$-30x = -15$$

$$x = \frac{1}{2}$$

($\frac{1}{2}, -2$)

$$10. \begin{cases} 3x + 5y = 2 & (3) \\ 2x - 3y = 14 & (5) \\ 9x + 15y = 6 \\ 10x - 15y = 70 \end{cases}$$

$19x = 76$

$\boxed{x = 4}$

$$\begin{array}{rcl} 2(4) - 3y & = & 14 \\ 8 - 3y & = & 14 \\ -3y & = & 6 \\ \boxed{y = -2} & & \end{array}$$

$$\boxed{(4, -2)}$$

$$11. \begin{cases} 4x - 6y = 7 \\ -2x + 3y = 0 & (2) \\ -4x + 6y = 0 \\ 0 + 0 = 7 \end{cases}$$

$0 \neq 7$ $\boxed{\emptyset}$ No solution

$$13. \begin{cases} 3(2x+y) = 4x+20 \\ x - 2y = 3 \end{cases}$$

$x = (2y+3)$ Substitution

$$\begin{aligned} 3(2(2y+3)+y) &= 4(2y+3)+20 \\ 3(4y+6+y) &= 8y+12+20 \\ 12y+18+3y &= 8y+32 \\ 15y+18 &= 8y+32 \\ \cancel{-8y} & \quad \cancel{-8y} \\ \hline 7y &= 14 \\ \boxed{y=2} & \end{aligned}$$

$$\begin{array}{rcl} x - 2(2) & = & 3 \\ x - 4 & = & 3 \\ \cancel{+4} & \quad \cancel{+4} \\ \hline x & = & 7 \end{array}$$

$\boxed{(7, 2)}$

$$12. \begin{cases} 3x + y = 7 & y = (-3x+7) \\ 4x + 3y = 1 & \text{substitution} \end{cases}$$

$$\begin{aligned} 4x + 3(-3x+7) &= 1 \\ 4x - 9x + 21 &= 1 \\ -5x + 21 &= 1 \\ -5x &= -20 \\ \boxed{x=4} & \end{aligned}$$

$3(4) + y = 7$
 $12 + y = 7$
 $\boxed{y = -5}$

$\boxed{(4, -5)}$

cross multiply

$$14. \begin{cases} \frac{x-3}{2} = \frac{2-y}{4} \\ \frac{7-2x}{3} = \frac{y}{2} \end{cases}$$

$$\begin{cases} 4(x-3) = 2(2-y) \\ 3y = 2(7-2x) \\ 4x-12 = 24-2y \\ 3y = 14-4x \end{cases}$$

$$4x = (-3y + 14)$$

$$-3y + 14 - 12 = 4 - 2y$$

$$-3y + 2 = 4 - 2y$$

$$2 = 4 + y$$

$$\boxed{-2 = y}$$

$$\frac{x-3}{2} = \frac{2-(-2)}{4}$$

$$\frac{x-3}{2} = \frac{4}{4}$$

$$\frac{x-3}{2} = 1$$

$$\boxed{(5, -2)}$$

$$\begin{cases} x-3=2 \\ \boxed{x=5} \end{cases}$$

Texashas 252,500 farms, and Missouri has 112,500 farms.

$$15. \begin{array}{l} x = 1^{\text{st}} \# \\ y = 2^{\text{nd}} \# \end{array}$$

$$\begin{cases} x+y=124 \\ x-y=32 \\ 2x=156 \\ \boxed{x=78} \end{cases}$$

elimination
 $78+y=124$
 $\boxed{y=46}$

$(78, 46)$

1st # is 78, and the second # is 46.

16. OMIT

17. $x = \# \text{ of farms in Texas}$
 $y = \# \text{ of farms in MO}$

$$\begin{cases} 140,000 + y = x \\ x + y = 365,000 \end{cases}$$

$$140,000 + y + y = 365,000$$

$$140,000 + 2y = 365,000$$

$$2y = 225,000$$

$$\boxed{y = 112,500}$$

$$x + 112,500 = 365,000$$

$$\boxed{x = 252,500}$$