

Chapter 4 Test Review p. 304

$$1. \begin{cases} 2x - 3y = 12 \\ 3x + 4y = 1 \end{cases}$$

$$a) 2(12) - 3(4) = 12 \\ 24 - 12 = 12 \quad \checkmark$$

$$b) 2(3) - 3(-2) = 12 \\ 6 + 6 = 12 \quad \checkmark$$

$$c) 2(-3) - 3(6) = 12 \\ -6 - 18 = 12 \quad \times$$

$$3(12) + 4(4) = 1 \\ 36 + 12 = 1 \quad \times$$

$$3(3) + 4(-2) = 1 \\ 9 - 8 = 1 \quad \checkmark$$

NO

NO

Yes

$$2. \begin{cases} 4x + y = 0 \\ -8x - 5y = 9 \end{cases}$$

$$a) 4\left(\frac{3}{4}\right) + (-3) = 0 \\ 3 + -3 = 0 \quad \checkmark$$

$$-8\left(\frac{3}{4}\right) - 5(-3) = 9 \\ -6 + 15 = 9$$

$$b) 4(-2) + 8 = 0 \\ -8 + 8 = 0$$

$$-8(-2) - 5(8) = 9 \\ 16 - 40 = 9$$

$$c) 4\left(\frac{1}{2}\right) - 2 = 0 \\ 2 - 2 = 0$$

$$-8\left(\frac{1}{2}\right) - 5(-2) = 9 \\ -4 + 10 = 9$$

Yes

NO

NO

$$3. \begin{cases} 5x - 6y = 18 \\ 2y - x = -4 \end{cases}$$

$$a) 5(-6) - 6(-8) = 18 \\ -30 + 48 = 18$$

$$2(-8) - (-6) = -4 \\ -16 + 6 = -4$$

$$b) 5(3) - 6\left(\frac{5}{2}\right) = 18 \\ 15 - 15 = 18 \quad \times$$

$$c) 5(3) - 6\left(-\frac{1}{2}\right) = 18 \\ 15 + 3 = 18$$

NO

NO

Yes

$$4. \begin{aligned} 2x + 3y &= 1 \\ 3y - x &= 4 \end{aligned}$$

$$a) 2(2) + 3(2) = 1$$

NO

$$b) 2(-1) + 3(1) = 1$$

$$3(1) - (-1) = 4$$

Yes

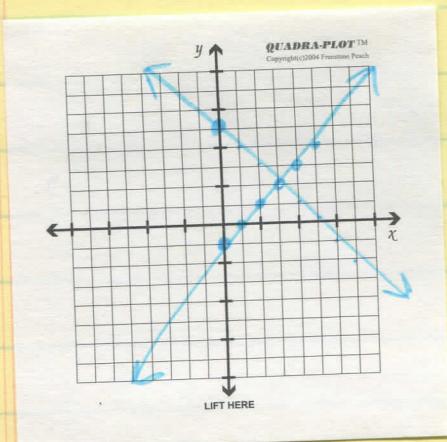
$$4 - 3 = 1 \checkmark$$

$$-3 - 2 \neq 4$$

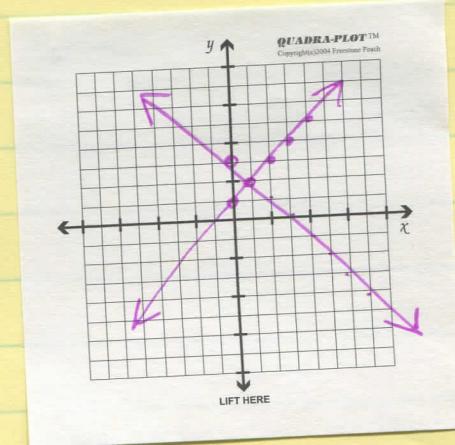
NO

$$5. \begin{cases} x + y = 5 \\ x - y = 1 \end{cases} \quad \begin{aligned} y &= -x + 5 \\ y &= x - 1 \end{aligned}$$

$$6. \begin{cases} x + y = 3 \\ x - y = -1 \end{cases} \quad \begin{aligned} y &= -x + 3 \\ y &= x + 1 \end{aligned}$$



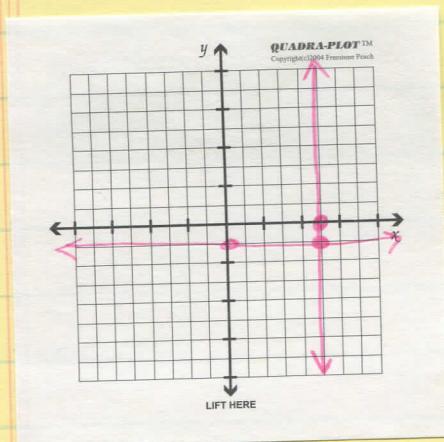
(3, 2)



(1, 2)

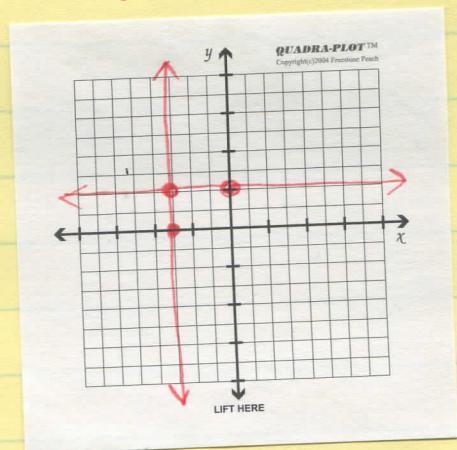
$$7. \begin{cases} x = 5 \\ y = -1 \end{cases}$$

(5, -1)

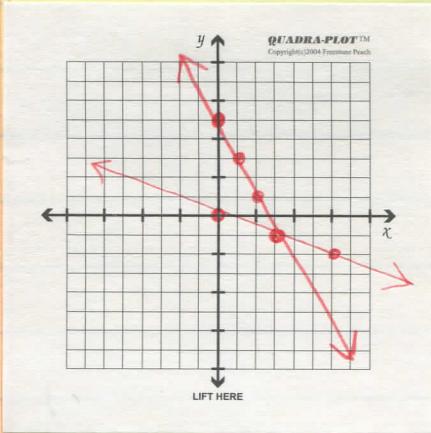


$$8. \begin{cases} x = -3 \\ y = 2 \end{cases}$$

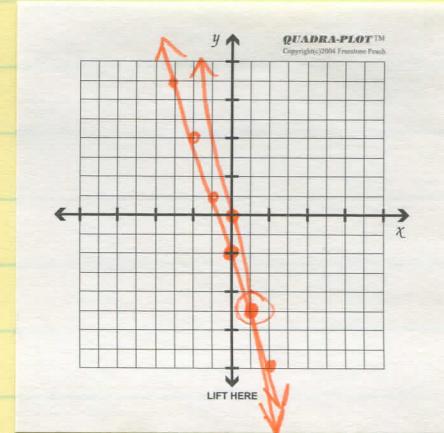
(-3, 2)



$$9. \begin{cases} 2x + y = 5 \\ x = -3y \end{cases} \quad y = -2x + 5 \quad 10. \begin{cases} 3x + y = -2 \\ y = -5x \end{cases} \quad y = -3x - 2$$

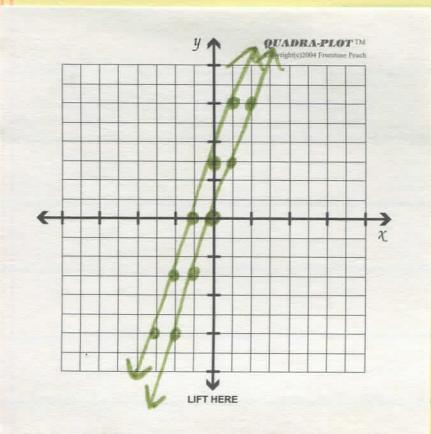


$$\boxed{(3, -1)}$$



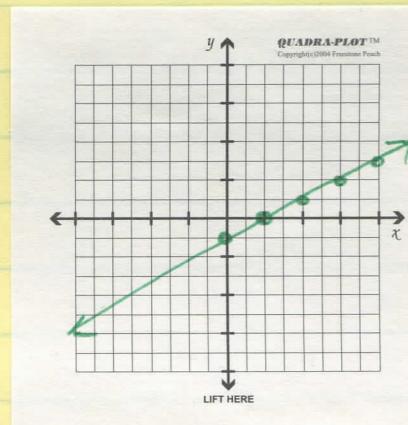
$$\boxed{(1, -5)}$$

$$11. \begin{cases} y = 3x \\ -6x + 2y = 6 \end{cases} \quad y = 3x + 3$$



$$\boxed{\emptyset} \\ // \leftrightarrow$$

$$12. \begin{cases} x - 2y = 2 \\ -2x + 4y = -4 \end{cases} \quad y = \frac{1}{2}x - 1$$



$$\boxed{\infty}$$

coinciding
↔

$$13. \begin{aligned} y &= 2x + 6 \\ 3x - 2y &= -11 \end{aligned}$$

$$3x - 2(2x + 6) = -11$$

$$3x - 4x - 12 = -11$$

$$-x - 12 = -11$$

$$-x = 1$$

$$\boxed{x = -1}$$

$$\boxed{y = 4}$$

$$y = 2(-1) + 6$$

$$= -2 + 6 = 4 \quad \boxed{(-1, 4)}$$

$$14. \begin{cases} y = 3x - 7 \\ 2x - 3y = 7 \end{cases}$$

$$2x - 3(3x - 7) = 7$$

$$2x - 9x + 21 = 7$$

$$-7x + 21 = 7$$

$$-7x = -14$$

$$\boxed{x = 2}$$

$$y = 3(2) - 7$$

$$= 6 - 7$$

$$\boxed{y = -1}$$

$$\boxed{(2, -1)}$$

$$15. \begin{cases} x + 3y = -3 \\ 2x + y = 4 \end{cases}$$

$$y = -2x + 4$$

$$x + 3(-2x + 4) = -3$$

$$\underline{x - 6x + 12 = -3}$$

$$-5x + 12 = -3$$

$$\underline{-5x = -15}$$

$$\boxed{x = 3}$$

$$3 + 3y = -3$$

$$\underline{3y = -6}$$

$$\boxed{y = -2}$$

$\boxed{(3, -2)}$

$$17. \begin{cases} 4y = 2x + 6 \\ x - 2y = -3 \end{cases}$$

$$x = 2y - 3$$

$$4y = 2(2y - 3) + 6$$

$$4y = 4y - 6 + 6$$

$$4y = 4y$$

$$\boxed{\infty}$$

infinitely many solutions

$$16. \begin{cases} 3x + y = 11 \\ x + 2y = 12 \end{cases}$$

$$x + 2(-3x + 11) = 12$$

$$\underline{x - 6x + 22 = 12}$$

$$-5x + 22 = 12$$

$$\underline{-5x = -10}$$

$$\boxed{x = 2}$$

$\boxed{(2, 5)}$

$$2 + 2y = 12$$

$$2y = 10$$

$$\boxed{y = 5}$$

$$18. \begin{cases} 9x = 6y + 3 \\ 6x - 4y = 2 \end{cases}$$

$$6\left(\frac{2}{3}y + \frac{1}{3}\right) - 4y = 2$$

$$\underline{4y + 2 - 4y = 2}$$

$$2 = 2$$

$\boxed{\infty}$

infinitely many solutions

$$19. \begin{cases} x + y = 6 \\ y = x - 4 \end{cases}$$

$$\cancel{x + (x - 4)} = 6$$

$$-4 \neq 6 \quad \times$$

$\boxed{\emptyset}$ no solution

$$20. \begin{cases} -3x + y = 6 \\ y = 3x + 2 \end{cases}$$

$$\cancel{-3x + (3x + 2)} = 6$$

$$2 \neq 6 \quad \times$$

$\boxed{\emptyset}$ no solution

$$21. \begin{cases} 2x + 3y = -6 \\ x - 3y = -12 \end{cases}$$

$$3x = -18$$

$$\boxed{x = -6}$$

$$-6 - 3y = -12$$

$$-3y = -6$$

$$\boxed{y = 2}$$

$$\boxed{(-6, 2)}$$

$$22. \begin{cases} 4x + y = 15 \\ 4x + 3y = -19 \end{cases}$$

$$4y = -4$$

$$\boxed{y = -1}$$

$$4x + (-1) = 15$$

$$4x = 16$$

$$\boxed{x = 4}$$

$$\boxed{(4, -1)}$$

$$23. \begin{cases} 2x - 3y = -15 \\ x + 4y = 31 \end{cases}$$

$$2x - 3y = -15$$

$$-2x - 8y = -62$$

$$-11y = -77$$

$$\boxed{y = 7}$$

$$x + 4(7) = 31$$

$$x + 28 = 31$$

$$\boxed{x = 3}$$

$$\boxed{(3, 7)}$$

$$24. \begin{cases} x - 5y = -22 \quad (-4) \\ 4x + 3y = 4 \end{cases}$$

$$-4x + 20y = 88$$

$$+ 4x + 3y = 4$$

$$23y = 92$$

$$\boxed{y = 4}$$

$$x - 5(4) = -22$$

$$x - 20 = -22$$

$$\boxed{x = -2}$$

$$\boxed{(-2, 4)}$$

$$25. \begin{cases} 2x - 6y = -1 \\ -x + 3y = \frac{1}{2} \end{cases}$$

$$2x - 6y = -1$$

$$-2x + 6y = 1$$

$$0 = 0 \checkmark$$

infinitely many solutions

$$26. \begin{cases} 0.16x - 0.3y = -1.5 \quad (10) \\ 0.04x - 0.02y = -0.1 \quad (100) \end{cases}$$

$$(2) \begin{cases} 6x - 3y = -15 \\ 4x - 2y = -10 \end{cases}$$

$$-12x + 6y = 30$$

$$+ 12x - 6y = -30$$

$$0 = 0 \checkmark$$

Infinitely many solutions

$$27. \begin{cases} \frac{3}{4}x + \frac{2}{3}y = 2 \\ x + \frac{4}{3}y = 6 \end{cases} \quad (1) \quad (2)$$

$$\begin{aligned} -3 & \begin{cases} 9x + 8y = 24 \\ 3x + y = 18 \end{cases} \\ & \begin{aligned} 9x + 8y &= 24 \\ -9x - 3y &= -54 \end{aligned} \\ & \underline{5y = -30} \\ & \boxed{y = -6} \end{aligned}$$

$$\begin{aligned} x + \frac{-6}{3} &= 6 \\ x - 2 &= 6 \\ \boxed{x = 8} \end{aligned} \quad \boxed{(8, -6)}$$

29-36 SKIP

$$37. \begin{cases} x + y = 16 \\ 3x - y = 72 \end{cases}$$

$$\begin{aligned} 4x &= 88 \\ \boxed{x = 22} \end{aligned}$$

$$\begin{aligned} 22 + y &= 16 \\ \boxed{y = -16} \end{aligned}$$

The two numbers
are -16 & 22 .

$$28. \begin{cases} 10x + 2y = 0 \\ 3x + 5y = 33 \end{cases} \quad (5) \quad (-2)$$

$$\begin{aligned} 50x + 10y &= 0 \\ -6x - 10y &= -66 \end{aligned}$$

$$\begin{aligned} 44x &= -66 \\ x &= \frac{-66}{44} \div 11 = \frac{6}{4} \div 2 = \boxed{\frac{3}{2}} \end{aligned}$$

$$\begin{aligned} 10\left(\frac{3}{2}\right) + 2y &= 0 \\ -15 + 2y &= 0 \\ 2y &= +15 \\ \boxed{y = +\frac{15}{2}} \end{aligned} \quad \boxed{\left(\frac{3}{2}, +\frac{15}{2}\right)}$$

$$38. \begin{cases} x + y = 360 \\ 45x + 35y = 15,150 \end{cases} \quad y = 360 - x$$

$$\begin{aligned} 45x + 35(360 - x) &= 15,150 \\ 45x + 12,600 - 35x &= 15,150 \end{aligned}$$

$$\begin{aligned} 10x &= 2550 \\ \boxed{x = 255} \end{aligned}$$

$$\begin{aligned} 255 + y &= 360 \\ \boxed{y = 105} \end{aligned}$$

Orchestra section tickets ~~sold out~~
255 and balcony section sold
105 tickets.

$$39. \begin{aligned} 340 &= 19x - 19y \\ 340 &= 14x + 14y \end{aligned}$$

OMIT

Each egg is \$0.40
and a strip of bacon \$0.65.

$$41. \begin{cases} 3x + 4y = 3.8 & (2) \\ 2x + 3y = 2.75 & (3) \end{cases}$$

$$\begin{array}{r} -6x - 8y = -7.6 \\ +6x + 9y = 8.25 \\ \hline y = 0.65 \end{array}$$

$$\begin{aligned} 2x + 3(0.65) &= 2.75 \\ 2x + 1.95 &= 2.75 \end{aligned}$$

$$\begin{aligned} 2x &= 0.80 \\ x &= 0.4 \end{aligned}$$

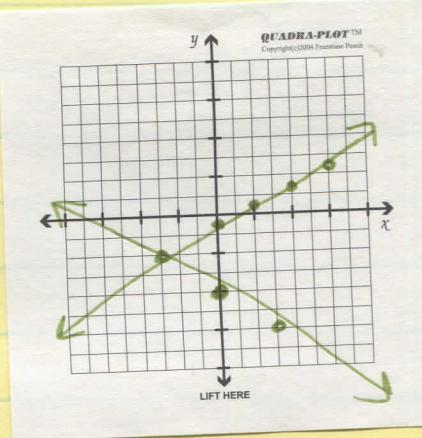
$$45. \begin{aligned} x + x + y &= 73 \\ \begin{cases} 2x + y = 73 \\ y = x + 7 \end{cases} \\ 2x + (x+7) &= 73 \\ 3x + 7 &= 73 \\ 3x &= 66 \\ x &= 22 \end{aligned}$$

$$\begin{aligned} y &= 22 + 7 \\ y &= 29 \end{aligned}$$

The two equal sides are 22 cm & the third side is 29cm.

$$47. \begin{cases} x - 2y = 1 \\ 2x + 3y = -12 \end{cases}$$

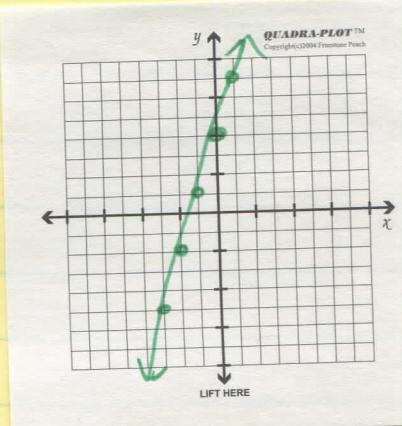
$$\begin{aligned} ① y &= \frac{1}{2}x - \frac{1}{2} \\ ② y &= -\frac{2}{3}x - 4 \\ (-3, -2) & \end{aligned}$$



$$48. \begin{cases} 3x - y = -4 \\ 6x - 2y = -8 \end{cases}$$

$$\begin{aligned} ① y &= 3x + 4 \\ ② y &= 3x + 4 \end{aligned}$$

∞
coinciding lines



$$49. \begin{cases} x + 4y = 11 \\ 5x - 9y = -3 \\ x = -4y + 11 \end{cases}$$

$$5(-4y + 11) - 9y = -3 \\ -20y + 55 - 9y = -3 \\ -29y = -58$$

$$y = 2$$

$$x + 4(2) = 11$$

$$x + 8 = 11$$

$$x = 3$$

$$(3, 2)$$

$$50. \begin{cases} x + 9y = 16 \\ 3x - 8y = 13 \end{cases} \quad (-3)$$

$$\begin{array}{r} 3x - 8y = 13 \\ 3x - 27y = -48 \\ \hline 35y = -35 \end{array}$$

$$35y = -35$$

$$\begin{array}{r} y = 1 \\ x + 9(1) = 16 \\ x = 7 \end{array}$$

$$(7, 1)$$

$$51. \begin{cases} y = -2x \\ 4x + 7y = -15 \end{cases}$$

$$4x + 7(-2x) = -15$$

$$4x - 14x = -15$$

$$-10x = -15$$

$$x = \frac{-15}{10} \div 5 = \frac{+3}{2}$$

$$\left(\frac{3}{2}, -3\right)$$

$$52. \begin{cases} 3y = 2x + 15 \\ -2x + 3y = 21 \end{cases}$$

$$\begin{array}{r} 2x - 3y = -15 \\ 8 \neq 6 \quad x \end{array}$$

\emptyset No solution

$$y = -2\left(\frac{3}{2}\right) = -3$$

$$54. \begin{cases} x + y = 19 \\ x - y = -3 \end{cases}$$

$$\frac{2x}{2} = \frac{16}{2}$$

$$x = 8$$

$$\begin{array}{r} -8 + y = -8 \\ y = 11 \end{array}$$

$$53. \begin{cases} 3x - y = 4 \\ 4y = 12x - 16 \end{cases}$$

$$y = 3x - 4$$

$$\begin{array}{r} -y = -3x + 4 \\ -1 \quad -1 \end{array}$$

$$y = 3x - 4$$

∞
coincident lines

$$(8, 11)$$

$$55. \begin{cases} x - 3y = -11 & (-1) \\ 4x + 5y = -10 \\ -4x + 12y = 44 \\ 17y = 34 \\ y = 2 \end{cases}$$

$x - 3(2) = -11$

$\cancel{x} - \cancel{6} = -11$

$x = -5$

$\boxed{(-5, 2)}$

$$56. \begin{cases} -x - 15y = 44 & (2) \\ 2x + 3y = 20 \\ -2x - 30y = 88 \\ -27y = 108 \\ y = -4 \end{cases}$$

$$\begin{aligned} -x - 15(-4) &= 44 \\ -x + 60 &= 44 \\ -x &= -16 \\ x &= 16 \end{aligned}$$

$\boxed{(16, -4)}$

$$58. \begin{cases} x - 4y = 4 \\ \frac{1}{8}x - \frac{1}{2}y = 3 & (8) \end{cases}$$

$(-1) \begin{cases} x - 4y = 4 \\ x - 4y = 24 \end{cases}$

$0 \neq 20 \times$

$\boxed{\emptyset}$ no solution

$$59. \begin{cases} x + y = 12 & (1) \\ 3x + y = 20 \\ 2x = 8 \\ x = 4 \end{cases}$$

$4 + y = 12$

$y = 8$

$x = 1^{\text{st}} \#$

$y = 2^{\text{nd}} \#$

$\boxed{\text{The two #'s are } 4 \text{ & } 8.}$

$$60. \begin{cases} x - y = -18 & (1) \\ 2x - y = -23 & (2) \end{cases}$$

$x = 1^{\text{st}} \#$

$y = 2^{\text{nd}} \#$

$x = -5$

$-5 - y = -18$

$-y = -13$

$y = 13$

$\boxed{\text{The two #'s are } -5 \text{ & } 13.}$

61. $x = \# \text{ of nickels}$
 $y = \# \text{ of dimes}$

$$\begin{cases} x + y = 65 & y = -x + 65 \\ 0.05x + 0.1y = 5.30 \end{cases}$$

$$0.05x + 0.1(-x + 65) = 5.30$$

$$0.05x + (0.1x + 6.5) = 5.30$$

$$-0.05x + 6.5 = 5.3$$

$$-0.05x = -1.2$$

$$\boxed{x = 24}$$

$$24 + y = 65$$

$$\boxed{y = 41}$$

Emma has 24 nickels
and 41 dimes.

62. $x = \# \text{ of } 49\text{¢ stamps}$
 $y = \# \text{ of } 34\text{¢ stamps}$

$$\begin{cases} x + y = 26 & y = -x + 26 \\ 0.49x + 0.34y = 11.39 \\ 0.49(x) + 0.34(-x + 26) = 11.39 \\ 0.49x - 0.34x + 8.84 = 11.39 \\ 0.15x = 2.55 \\ \boxed{x = 17} \end{cases}$$

$$\begin{cases} 17 + y = 26 \\ \boxed{y = 9} \end{cases}$$

Sarah and Owen purchased
17 49¢ stamps and
9 34¢ stamps.