

Show all work!

46 total

## Factoring Practice

### I. Greatest Common Factor (GCF)

Find the GCF of the numbers.

$$\begin{aligned}18, 30 \\ 18 &= 2 \cdot 3 \cdot 3 \\ 30 &= 2 \cdot 3 \cdot 5 \\ 2 \cdot 3 &= 6 \\ 6 &= \text{GCF}\end{aligned}$$

1. 12, 18
2. 10, 35
3. 8, 30
4. 16, 24
5. 28, 49
6. 27, 63
7. 30, 45
8. 48, 72

Pick 4 of the 8

### II. Greatest Common Monomial Factor

Factor, write prime if prime.

$$12a^3b + 15ab^3 = 3ab(4a^2 + 5b^2)$$

1.  $6x + 3$
2.  $24x^2 - 8x$
3.  $6x - 12$
4.  $2x^2 + 8x$
5.  $4x + 10$
6.  $10x^2 + 35x$
7.  $10x^2y - 15xy^2$
8.  $12x^2 - 9x + 15$
9.  $3n^3 - 12n^2 - 30n$
10.  $9m^2 - 4n + 12$
11.  $2x^3 - 3x^2 + 5x$
12.  $13m + 26m^2 - 39m^3$
13.  $17x^2 + 34x + 51$
14.  $18m^2n^4 - 12m^2n^3 + 24m^2n^2$

Pick 5 of the 14

### III. Factoring the Difference of Two Squares

$$\begin{aligned}a^2 - 36 &= (a + 6)(a - 6) \\ 3x^2 - 48 &= 3(x^2 - 16) = 3(x + 4)(x - 4)\end{aligned}$$

Factor, write prime if prime.

1.  $x^2 - 1$
2.  $x^2 - 9$
3.  $x^2 + 4$
4.  $x^2 - 25$
5.  $9y^2 - 16$
6.  $4x^2 - 25$
7.  $9x^2 - 1$
8.  $a^2 - x^2$
9.  $25 - m^2$
10.  $x^2 - 16y^2$
11.  $25m^2 - n^2$
12.  $-x^2 + 16$
13.  $36m^2 - 121$
14.  $2x^2 - 8$
15.  $25 + 4x^2$
16.  $4a^2 - 81b^2$
17.  $12x^2 - 75$
18.  $a^2b - b^3$
19.  $-98 + 2x^2$
20.  $5x^2 - 45y^2$
21.  $9x^4 - 4$
22.  $16x^4 - y^2$

Pick 7 of the 22

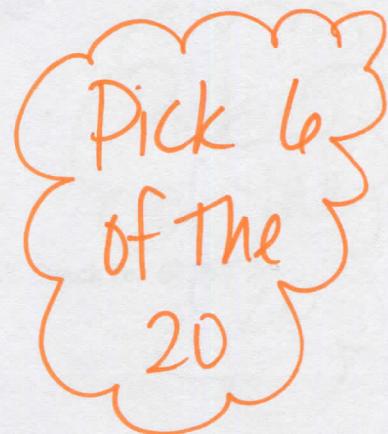
#### IV. Factoring Perfect Square Trinomials

$$x^2 - 14x + 49 = (x - 7)^2$$

Factor, write prime if prime.

1.  $x^2 + 8x + 16$
2.  $x^2 - 16x + 64$
3.  $y^2 + 12y + 36$
4.  $a^2 - 10a + 25$
5.  $16y^2 + 8y + 1$
11.  $25a^2 + 60a + 36$
12.  $16 + 40x + 25x^2$
13.  $16x^2 + 24x + 9$
14.  $49x^2 - 14x + 1$
15.  $9y^2 - 30y + 25$

6.  $9x^2 - 6x + 1$
7.  $25x^2 + 10x + 1$
8.  $n^2 - 14n + 49$
9.  $81x^2 - 90x + 25$
10.  $4y^2 - 20y + 25$
16.  $n^2 + 2n + 4$
17.  $b^2 + 2b + 1$
18.  $36x^2 + 84x + 49$
19.  $81 - 18x + x^2$
20.  $4 - 12y + 9y^2$

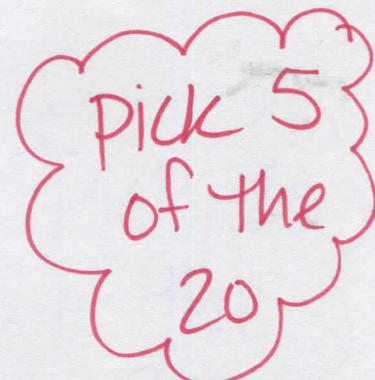


#### V. Special Factoring - Challenge

Factor, write prime if prime.

1.  $a^2 - 36$
2.  $9x^2 - 49$
3.  $169m^2 - 4u^2$
4.  $x^2y^2 - 9z^4$
5.  $\frac{1}{4}x^2 - 25y^2$
6.  $\frac{1}{9}x^2 - 16$
7.  $64 - a^4b^4$
8.  $y^6 - 100$
9.  $\frac{4}{9}x^2y^2 - \frac{25}{36}z^2$
10.  $y^8 - 81$

11.  $1 - 8u + 16u^2$
12.  $a^2b^2 + 6ab + 9$
13.  $x^2 + 2xy + y^2$
14.  $4x^2 + 12xy + 9y^2$
15.  $100h^2 + 20h + 1$
16.  $9a^2 - 24a + 16$
17.  $4a^3 + 8a^2 + 4a$
18.  $5c + 20c^2 + 20c^3$
19.  $(x + 4)^2 - (y + 1)^2$
20.  $(x - 1)^2 - 10(x - 1) + 25$



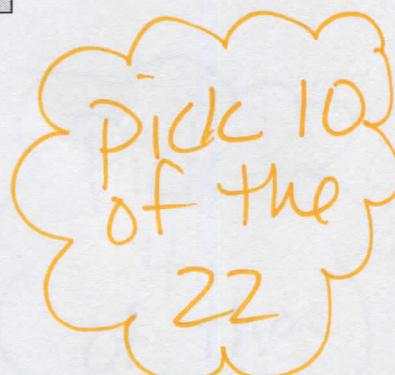
#### VI. Factoring Trinomials: $x^2 + bx + c$

$$x^2 + 7x + 10 = (x)^2 + (2 + 5)x + (2)(5) = (x + 2)(x + 5)$$

Factor, write prime if prime.

1.  $x^2 + 6x + 8$
2.  $c^2 + 5c + 6$
3.  $y^2 - 9y + 14$
4.  $x^2 - 10x + 16$
5.  $a^2 + 12a + 27$
6.  $x^2 - 14x + 24$
7.  $x^2 - 15x + 36$
8.  $y^2 + 21y + 54$
9.  $m^2 + 13m - 36$
10.  $x^2 - 8x + 15$
11.  $y^2 - 4y - 32$

12.  $x^2 - x - 6$
13.  $y^2 + 3y - 18$
14.  $b^2 + 7b - 18$
15.  $a^2 + a - 56$
16.  $c^2 - 4c - 12$
17.  $x^2 - 9x - 36$
18.  $y^2 + 4y - 21$
19.  $x^2 - 22x - 75$
20.  $x^2 - 3x - 40$
21.  $45 + 14y + y^2$
22.  $x^2 - 13x + 36$



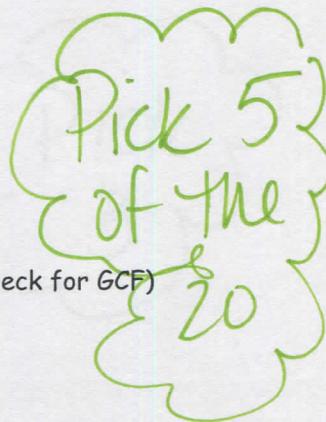
## VII. ...More Factoring Trinomials: $x^2 + bx + c$

$$k^2 - k - 20 = (k)^2 + (4 - 5)k + (4)(-5) = (k + 4)(k - 5)$$

Factor, write prime if prime.

1.  $x^2 + 7x + 12$
2.  $m^2 + 10m + 21$
3.  $y^2 - 7y - 8$
4.  $x^2 - 6x + 5$
5.  $x^2 + 4x - 32$
6.  $x^2 - 2x - 15$
7.  $x^2 - 6x + 8$
8.  $y^2 + 9y + 18$
9.  $3 - 4t + t^2$
10.  $v^2 + 12v + 20$

11.  $51 - 20k + k^2$
12.  $a^2 - 14ab + 24b^2$
13.  $y^2 + 6y - 72$
14.  $x^2 - 11xy - 60y^2$
15.  $15r^2 + 2rs - s^2$
16.  $3x^2 + 21xy - 54y^2$  (Hint: Check for GCF)
17.  $x^2 - 5xy - 6y^2$
18.  $x^2 + 8xy + 12y^2$
19.  $y^2 - 7xy + 10x^2$
20.  $a^2 - 11ab - 60b^2$



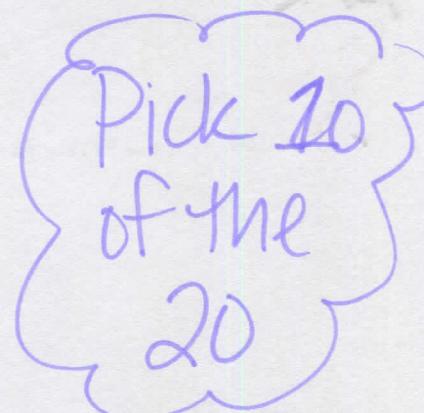
## VIII. Factoring Trinomials: $ax^2 + bx + c$

$$2x^2 - 5x - 3 = (2x + 1)(x - 3)$$

Factor, write prime if prime.

1.  $2x^2 - 5x - 3$
2.  $3x^2 + 10x - 8$
3.  $2y^2 + 15y + 7$
4.  $7a^2 - 11a + 4$
5.  $5n^2 + 17n + 6$
6.  $4y^2 + 8y + 3$
7.  $3x^2 + 4x - 7$
8.  $2x^2 + 13x + 15$
9.  $9y^2 + 6y - 8$
10.  $6x^2 - 7x - 20$

11.  $2n^2 - 3n - 14$
12.  $5n^2 + 2n + 7$
13.  $10x^2 + 13x - 30$
14.  $12y^2 + 7y + 1$
15.  $2n^2 + 9n - 5$
16.  $2x^2 + 7x + 6$
17.  $5a^2 - 42a - 27$
18.  $15x^2 - 28x - 32$
19.  $8a^2 - 10a + 3$
20.  $2y^2 - 3y - 20$

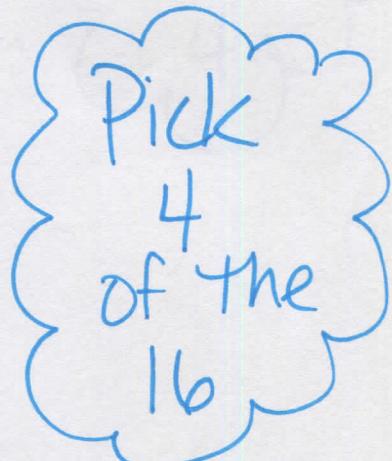


## IX. ...More Factoring Trinomials: $ax^2 + bx + c$

Factor, write prime if prime.

1.  $3x^2 + 4x + x$
2.  $5z^2 + 7z + 2$
3.  $2n^2 - 11n + 5$
4.  $3z^2 + z - 2$
5.  $5h^2 - 2h - 7$
6.  $8s^2 - 10st + 3t^2$
7.  $6x^2 + 19x + 15$
8.  $28a^2 + 5ab - 12b^2$

9.  $2a^2 + 7ab - 15b^2$
10.  $12x^2 + 17x + 6$
11.  $4a^2 - 4ab - 5b^2$
12.  $56y^2 + 15y - 56$
13.  $12x^2 - 29xy + 14y^2$
14.  $64x^2 + 32xy - 21y^2$
15.  $16x^2 + 56xy + 49y^2$
16.  $18x^2 - 57x + 35$



## X. Factoring: Putting It All Together

$$5x^2 + 20x - 60 = 5(x^2 + 4x - 12) = 5(x + 6)(x - 2)$$

Factor Completely, write prime if prime.

1.  $2x^2 - 8$
2.  $2x^2 + 8x + 6$
3.  $3n^2 + 9n - 30$
4.  $6x^2 - 26x - 20$
5.  $2x^2 + 12x - 80$
6.  $5t^2 + 15t + 10$
7.  $8n^2 - 18$
8.  $14x^2 + 7x - 21$

9.  $4x^2 + 16x + 16$
10.  $18x + 12x^2 + 2x^3$
11.  $2x - 2xy^2$
12.  $3t^3 - 27t$
13.  $24a^2 - 30a + 9$
14.  $10x^2 + 15x - 10$
15.  $3x^2 - 42x + 147$
16.  $4x^4 - 4x^2$



## XI. ...More Factoring: Putting It All Together

1.  $16x^2 - 40x - 24$
2.  $27x^2 - 36x + 12$
3.  $5x^2 - 60x - 140$
4.  $6m^3 + 54m^2 - 6m$
5.  $5k^4 + 8k^3 - 4k^2$
6.  $x^2y^4 - x^6$
7.  $y^4 - 6y^2 - 16$

8.  $x^4 - 3x^2 - 4$
9.  $h^2 - (a^2 - 6a + 9)$
10.  $81x^4 - 16y^4$
11.  $4mn^2 - 4m^2n^2 + m^3n^2$
12.  $(2a + 3)^2 - (a - 1)^2$
13.  $16d^8 - 8d^4 + 1$
14.  $x^2(x^2 - 4) + 4x(x^2 - 4) + 4(x^2 - 4)$



## XII. Extra: Factoring by Grouping

$$\begin{aligned} 6ax - 2b - 3a + 4bx &= 6ax - 3a + 4bx - 2b \\ &= 3a(2x - 1) + 2b(2x - 1) \\ &= (2x - 1)(3a + 2b) \end{aligned}$$

1.  $x^2 + 2x + xy + 2y$
2.  $3a^2 - 2b - 6a + ab$
3.  $t^3 - t^2 + t - 1$  Hint:  $t - 1 = 1(t - 1)$
4.  $10 + 2t - 5s - st$
5.  $\frac{2}{3}bc - \frac{14}{3}b + c - 7$
6.  $4u^2 + v + 2uv + 2u$
7.  $ad + 3a - d^2 - 3d$

8.  $n^2 + 2n + 3mn + 6m$
9.  $2ax^2 + bx^2 - 2ay^2 - by^2$
10.  $yz^2 - y^3 + z^3 - y^2z$
11.  $y^3 - y^2 - 4y + 4$
12.  $x^2a + x^2b - 16a - 16b$
13.  $x^3 + x^2 - x - 1$
14.  $a^3 - a^2 - 8a + 8$



## Factoring Practice Key

### I. Greatest Common Factor

1. 6
2. 5
3. 2
4. 8
5. 7
6. 9
7. 15
8. 24

### II. Greatest Common Monomial Factor

1.  $3(2x + 1)$
2.  $8x(3x - 1)$
3.  $6(x - 2)$
4.  $2x(x + 4)$
5.  $2(2x + 5)$
6.  $5x(2x + 7)$
7.  $5xy(2x - 3y)$
8.  $3(4x^2 - 3x + 5)$
9.  $3n(n^2 - 4n - 10)$
10. prime
11.  $x(2x^2 - 3x + 5)$
12.  $13m(1 + 2m - 3m^2)$
13.  $17(x^2 + 2x + 3)$
14.  $6m^2n^2(3n^2 - 2n + 4)$

### III. Factoring the Difference of Two Squares

1.  $(x + 1)(x - 1)$
2.  $(x + 3)(x - 3)$
3. prime
4.  $(x + 5)(x - 5)$
5.  $(3y + 4)(3y - 4)$
6.  $(2x + 5)(2x - 5)$
7.  $(3x + 1)(3x - 1)$
8.  $(a + x)(a - x)$
9.  $(5 + m)(5 - m)$
10.  $(x + 4y)(x - 4y)$
11.  $(5m + n)(5m - n)$
12.  $(4 + x)(4 - x)$
13.  $(6m + 11)(6m - 11)$
14.  $2(x + 2)(x - 2)$
15. prime
16.  $(2a + 9b)(2a - 9b)$
17.  $3(2x + 5)(2x - 5)$
18.  $b(a + b)(a - b)$
19.  $-2(7 + x)(7 - x)$  or  $2(x + 7)(x - 7)$
20.  $5(x + 3y)(x - 3y)$
21.  $(3x^2 + 2)(3x^2 - 2)$
22.  $(4x^2 + y)(4x^2 - y)$

### IV. Factoring Perfect Square Trinomials

1.  $(x + 4)^2$
2.  $(x - 8)^2$
3.  $(y + 6)^2$
4.  $(a - 5)^2$
5.  $(4y + 1)^2$
6.  $(3x - 1)^2$
7.  $(5x + 1)^2$

8.  $(n - 7)^2$
9.  $(9x - 5)^2$
10.  $(2y - 5)^2$
11.  $(5a + 6)^2$
12.  $(4 + 5x)^2$
13.  $(4x + 3)^2$
14.  $(7x - 1)^2$
15.  $(3y - 5)^2$
16. prime
17.  $(b + 1)^2$
18.  $(6x + 7)^2$
19.  $(x - 9)^2$
20.  $(3y - 2)^2$

### V. Special Factoring - Challenge

1.  $(a + 6)(a - 6)$
2.  $(3x + 7)(3x - 7)$
3.  $(13m + 2u)(13m - 2u)$
4.  $(xy + 3z^2)(xy - 3z^2)$
5.  $\left(\frac{1}{2}x + 5y\right)\left(\frac{1}{2}x - 5y\right)$
6.  $\left(\frac{1}{3}x + 4\right)\left(\frac{1}{3}x - 4\right)$
7.  $(8 + a^2b^2)(8 - a^2b^2)$
8.  $(y^3 + 10)(y^3 - 10)$
9.  $\left(\frac{2}{3}xy + \frac{5}{6}z\right)\left(\frac{2}{3}xy - \frac{5}{6}z\right)$
10.  $(y^4 + 9)(y^2 + 3)(y^2 - 3)$
11.  $(1 - 4u)^2$  or  $(4u - 1)^2$
12.  $(ab + 3)^2$
13.  $(x + y)^2$
14.  $(2x + 3y)^2$
15.  $(10h + 1)^2$
16.  $(3a - 4)^2$
17.  $4a(a + 1)^2$
18.  $5c(2c + 1)^2$
19.  $[(x + 4) + (y + 1)][(x + 4) - (y + 1)]$  or  $(x + y + 5)(x - y + 3)$
20.  $[(x - 1) - 5]^2$  or  $(x - 6)^2$

### VI. Factoring Trinomials: $x^2 + bx + c$

1.  $(x + 4)(x + 2)$
2.  $(c + 2)(c + 3)$
3.  $(y - 7)(y - 2)$
4.  $(x - 8)(x - 2)$
5.  $(a + 9)(a + 3)$
6.  $(x - 12)(x - 2)$
7.  $(x - 12)(x - 3)$
8.  $(y + 18)(y + 3)$
9. prime
10.  $(x - 5)(x - 3)$
11.  $(y - 8)(y + 4)$
12.  $(x - 3)(x + 2)$
13.  $(y + 6)(y - 3)$
14.  $(b + 9)(b - 2)$
15.  $(a + 8)(a - 7)$
16.  $(c - 6)(c + 2)$
17.  $(x - 12)(x + 3)$
18.  $(y + 7)(y - 3)$
19.  $(x - 25)(x + 3)$
20.  $(x - 8)(x + 5)$

21.  $(y+9)(y+5)$
22.  $(x-9)(x-4)$

### VII. ...More Factoring Trinomials: $x^2 + bx + c$

1.  $(x+4)(x+3)$
2.  $(m+3)(m+7)$
3.  $(y-8)(y+1)$
4.  $(x-1)(x-5)$
5.  $(x+8)(x-4)$
6.  $(x-5)(x+3)$
7.  $(x-2)(x-4)$
8.  $(y+3)(y+6)$
9.  $(t-1)(t-3)$
10.  $(v+2)(v+10)$
11.  $(3-k)(17-k)$  or  $(k-3)(k-17)$
12.  $(a-2b)(a-12b)$
13.  $(y-6)(y+12)$
14.  $(x-15y)(x+4y)$
15.  $(5r-s)(3r+s)$
16.  $3(x-2y)(x+9y)$
17.  $(x-6y)(x+y)$
18.  $(x+6y)(x+2y)$
19.  $(y-5x)(y-2x)$
20.  $(a-15b)(a+4b)$

### VIII. Factoring Trinomials: $ax^2 + bx + c$

1.  $(2x+1)(x-3)$
2.  $(3x-2)(x+4)$
3.  $(2y+1)(y+7)$
4.  $(7a-4)(a-1)$
5.  $(5n+2)(n+3)$
6.  $(2y+3)(2y+1)$
7.  $(3x+7)(x-1)$
8.  $(2x+3)(x+5)$
9.  $(3y-2)(3y+4)$
10.  $(3x+4)(2x-5)$
11.  $(2n-7)(n+2)$
12. prime
13.  $(2x+5)(5x-6)$
14.  $(3y+1)(4y+1)$
15.  $(2n-1)(n+5)$
16.  $(2x+3)(x+2)$
17.  $(5a+3)(a-9)$
18.  $(3x-8)(5x+4)$
19.  $(2a-1)(4a-3)$
20.  $(2y+5)(y-4)$

### IX. ...More Factoring Trinomials: $ax^2 + bx + c$

1.  $(3x+1)(x+1)$
2.  $(5z+2)(z+1)$
3.  $(2n-1)(n-5)$
4.  $(3z-2)(z+1)$
5.  $(5h-7)(h+1)$
6.  $(4s-3t)(2s-t)$
7.  $(2x+3)(3x+5)$
8.  $(7a-4b)(4a+3b)$
9.  $(2a-3b)(a+5b)$
10.  $(3x+2)(4x+3)$
11. prime
12.  $(7y+8)(8y-7)$
13.  $(4x-7y)(3x-2y)$
14.  $(8x+7y)(8x-3y)$

15.  $(4x+7y)^2$
16.  $(6x-5)(3x-7)$

### X. Factoring: Putting It All Together

1.  $2(x+2)(x-2)$
2.  $2(x+3)(x+1)$
3.  $3(n+5)(n-2)$
4.  $2(3x+2)(x-5)$
5.  $2(x+10)(x-4)$
6.  $5(t+1)(t+2)$
7.  $2(2n+3)(2n-3)$
8.  $7(2x+3)(x-1)$
9.  $4(x+2)^2$
10.  $2x(3+x)^2$  or  $2x(x+3)^2$
11.  $2x(1+y)(1-y)$
12.  $3t(t+3)(t-3)$
13.  $3(2a-1)(4a-3)$
14.  $5(2x-1)(x+2)$
15.  $3(x-7)^2$
16.  $4x^2(x+1)(x-1)$

### XI. ...More Factoring: Putting It All Together

1.  $8(2x+1)(x-3)$
2.  $3(3x-2)^2$
3.  $5(x-14)(x+2)$
4.  $6m(m^2+9m-1)$
5.  $k^2(5k-2)(k+2)$
6.  $x^2(y^2+x^2)(y+x)(y-x)$
7.  $(y^2-8)(y^2+2)$
8.  $(x^2+1)(x+2)(x-2)$
9.  $[h+(a-3)][h-(a-3)]$  or  $(h+a-3)(h-a+3)$
10.  $(9x^2+4y^2)(3x+2y)(3x-2y)$
11.  $mn^2(2-m)^2$  or  $mn^2(m-2)^2$
12.  $[(2a+3)+(a-1)][(2a+3)-(a-1)]$  or  $(3a+2)(a+4)$
13.  $(2d^2+1)^2(2d^2-1)^2$
14.  $(x+2)^3(x-2)$

### XII. Extra: Factoring by Grouping

1.  $(x+2)(x+y)$
2.  $(a-2)(3a+b)$
3.  $(t-1)(t^2+2)$
4.  $(5+t)(2-s)$
5.  $(c+7)\left(\frac{2}{3}b+1\right)$
6.  $(2u+1)(2u+v)$
7.  $(d+3)(a-d)$
8.  $(n+2)(n+3m)$
9.  $(x-y)(x+y)(2a+b)$
10.  $(z-y)(z+y)^2$
11.  $(y-1)(y+2)(y-2)$
12.  $(a+b)(x+4)(x-4)$
13.  $(x+1)^2(x-1)$
14.  $(a-1)(a^2-8)$